

# Power Architecture and Magnetics to Unlock the Potential of WBG Semiconductor Devices

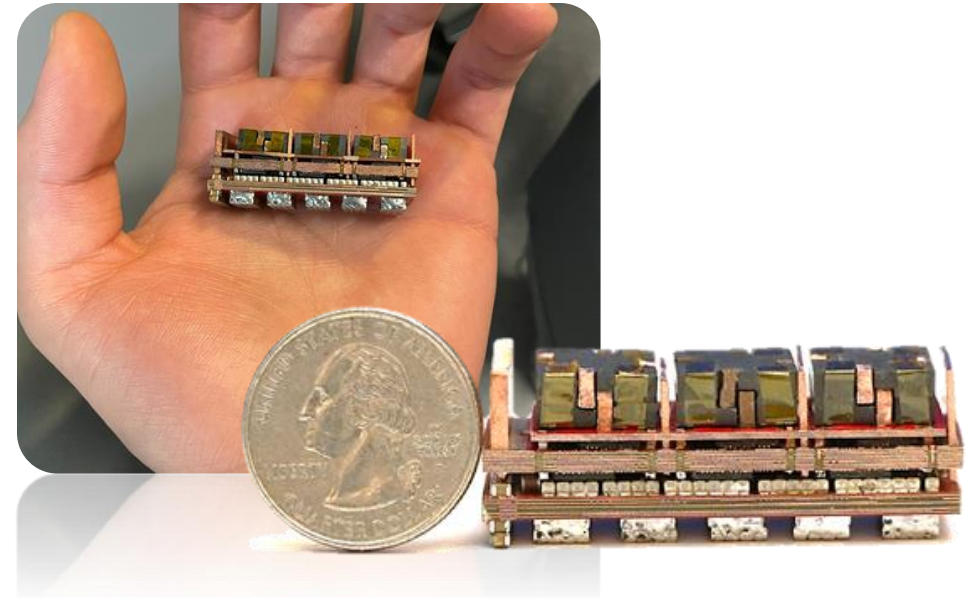
**Minjie Chen**

Assistant Professor

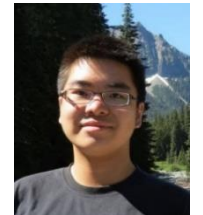
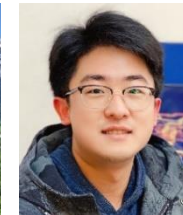
Electrical and Computer Engineering

Andlinger Center for Energy and the Environment

Princeton University



# Princeton Power Electronics Research Lab





# Emerging Trends in Power Electronics



**Grid-Forming  
Inverters**



**Cloud Computing and 5G**



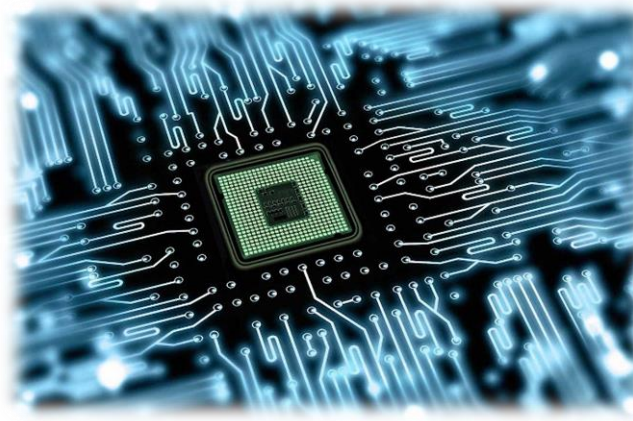
**Power for  
Robotics**

**Extreme Performance and Complex Functions**

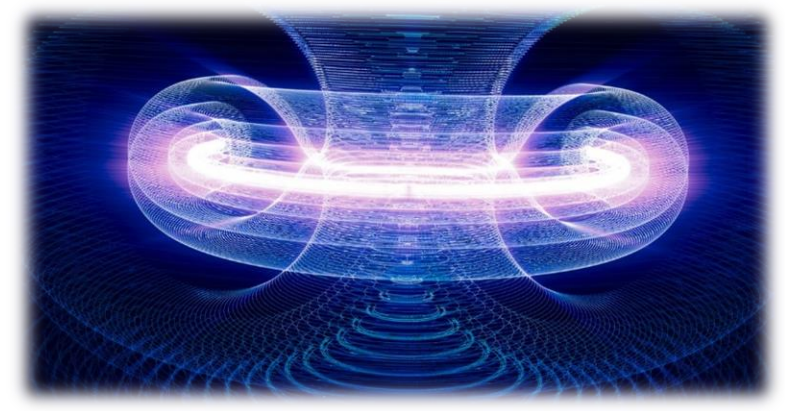
**Extreme High Density**



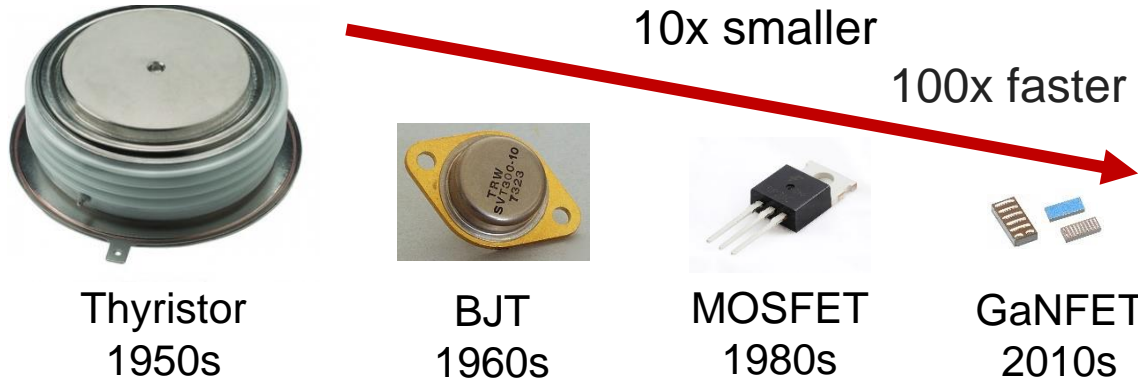
**Very High Efficiency**



**Extreme Environment**



## ➤ Opportunities - Rapid advances in semiconductors



## ➤ Switching at higher frequencies

- ❖ Reduces energy storage requirements
- ❖ Reduces passive component size
- ❖ L, C values  $\propto 1/f$

$$Z_L = j\omega L$$
$$Z_C = \frac{1}{j\omega C}$$

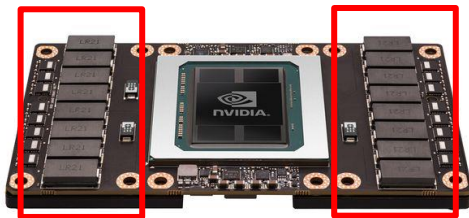
## ➤ Challenges - Passive components dominating the size

Ac-Dc Adapter



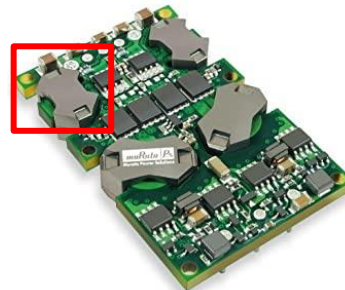
[Apple Ipad Adapter]

CPU Supply



[Nvidia Tesla V100]

Telecom Dc-Dc



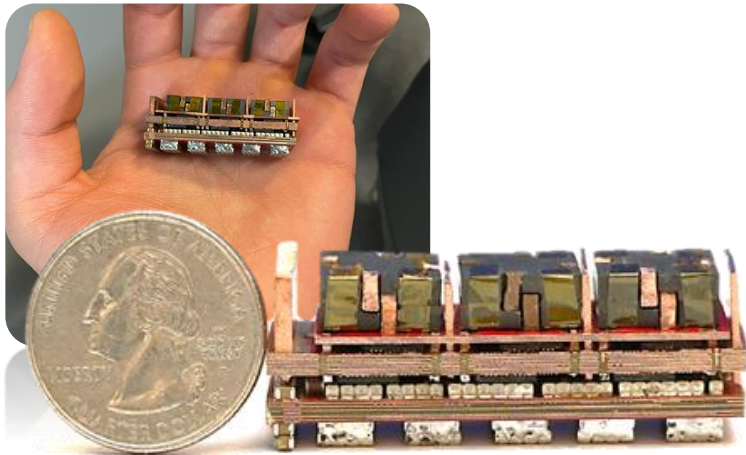
[Synqor PQ Series]

## ➤ Limitations of higher frequencies

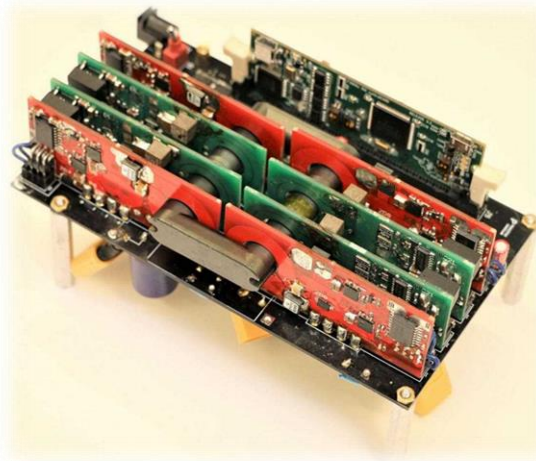
- ❖ Switching loss
- ❖ Core loss
- ❖ Material property
- ❖ Parasitics



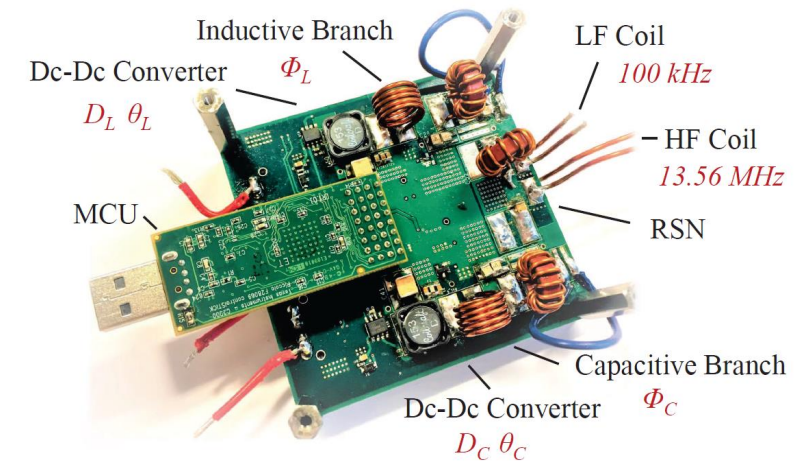
- **Extreme Performance:** Hybrid-Switched-Capacitor Architecture  
*Extreme Performance CPU Voltage Regulators*
- **Sophisticated Functions:** Control of MIMO Power Flow  
*Modeling and Control of Multiport Energy Routers*
- **Enabling New Applications:** Dual Frequency Wireless Power Transfer  
*Compensate for Impedance Variation with Reactance Steering Network*



CPU Voltage Regulator



MIMO Energy Router



Dual-Band Wireless Power Transfer

**Nvidia 8 x GPU AI Server**  
 **$230V_{AC} - 400V_{DC} - 48V_{DC} - 1V_{DC}, >10 \text{ kW}$**



**Nvidia Tesla A100**  
 **$48V - 1V, 1kA, 1kW$**

## Extreme performance 48V-1V PoL

### ➤ Processor-Level

- High current ( $>1,000 \text{ A/core}$ )
- High conversion ratio (48 V-1 V)
- Fast control bandwidth ( $>1 \text{ A/ns}$ )
- High density ( $>100 \text{ A/cm}^2$ )
- High efficiency ( $>95\%$ )

### ➤ Server-Level

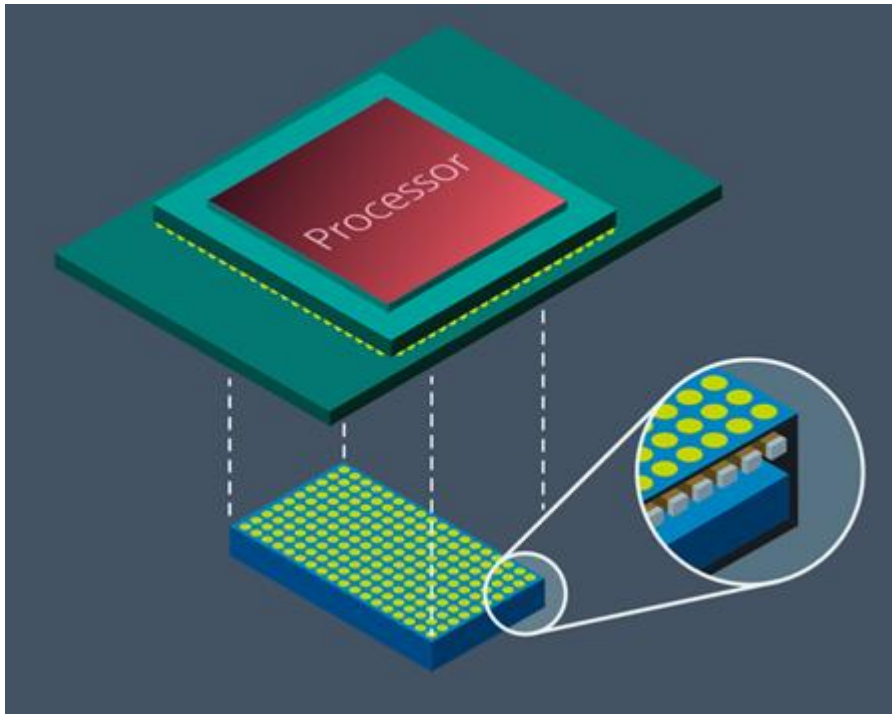
- Modular loads (up to 16 GPUs together)
- Core-to-core communications



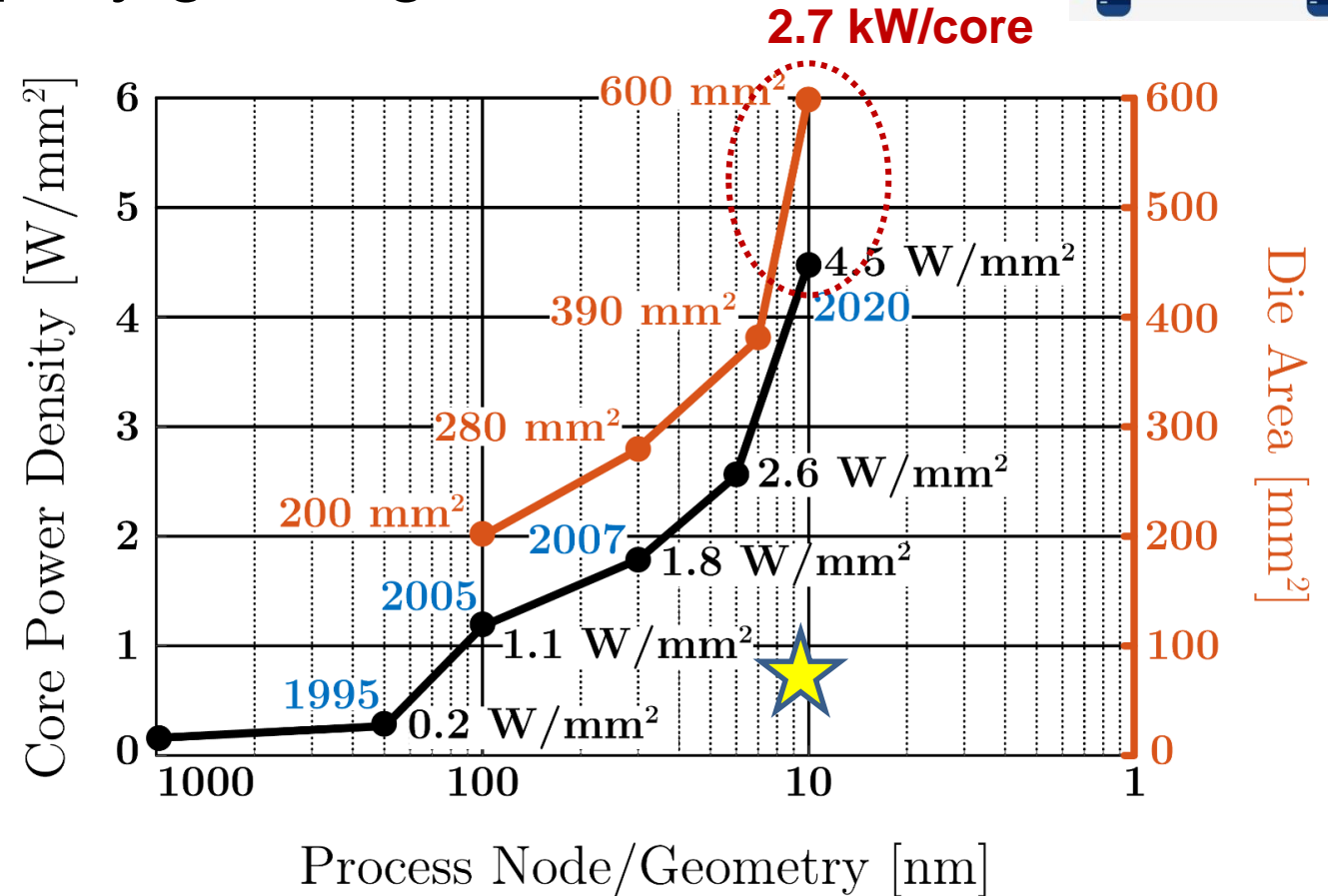


# Vertical Power Delivery for Microprocessors

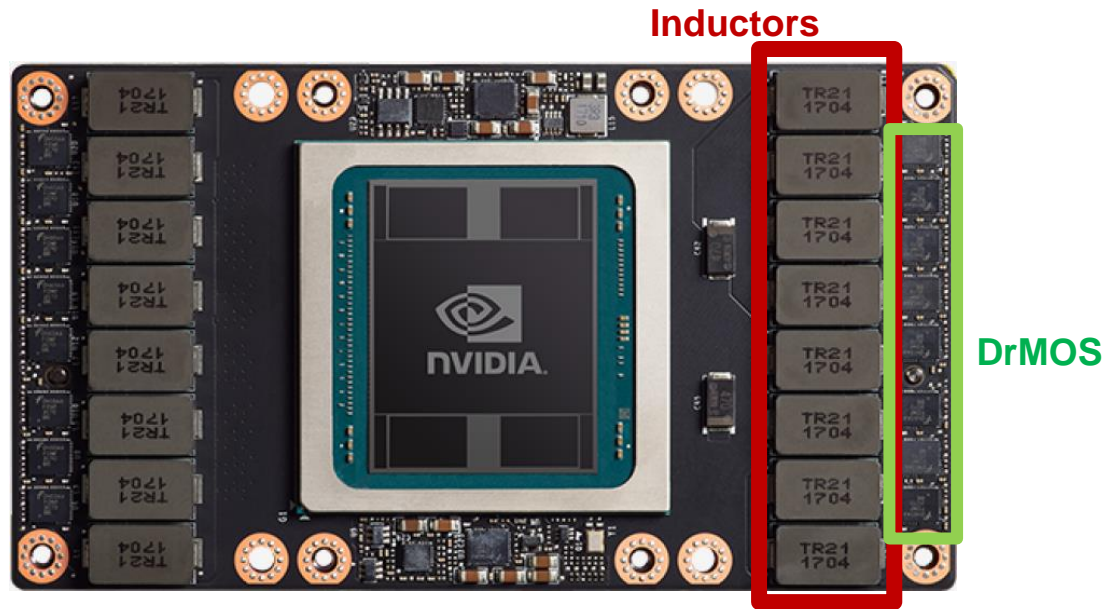
- Power consumption per core as high as 2 kW
- Silicon power density still rapidly growing ...



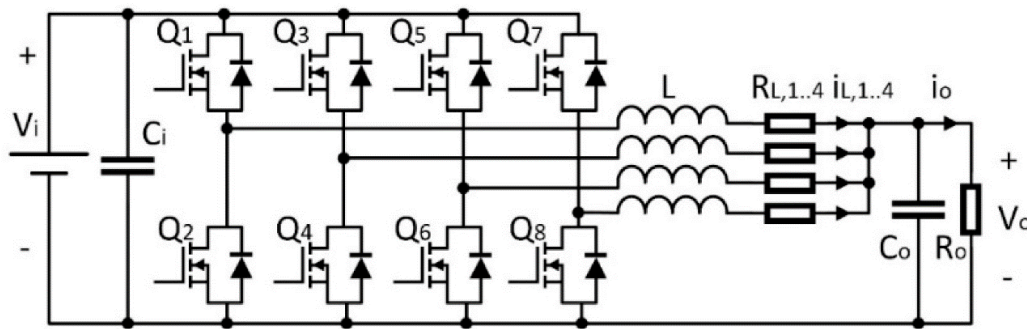
Vertical Power Delivery to Microprocessors



- J. Beak et al., “Vertical Stacked 48V-1V CPU Voltage Regulator with 91.1% Efficiency, 1 A/mm<sup>2</sup> Current Density and 1,000 W/in<sup>3</sup> Power Density”, IEEE Transactions on Power Electronics, in preparation.



Nvidia Tesla V100 Accelerator – 16 Phase Buck



## Traditional PoL Architectures

### ➤ Buck Derived Solutions

- High conversion ratio (48:1)
- Narrow ON/OFF
- Low duty ratio
- Poor inductance utilization
- Almost impossible to control

### ➤ Transformer Based Solutions

- High turns ratio (48:1)
- Complicated dynamics
- Difficult to do current mode control
- Transformer leakage and parasitics
- Lack of magnetics in MHz range

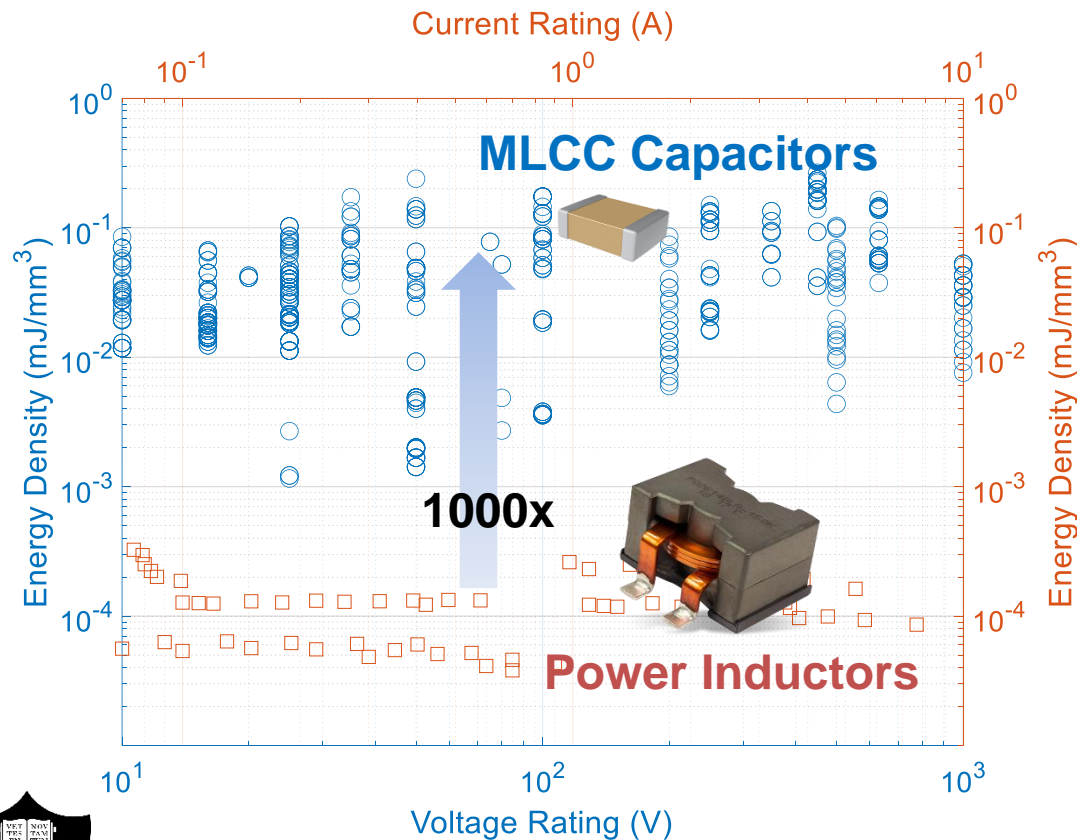




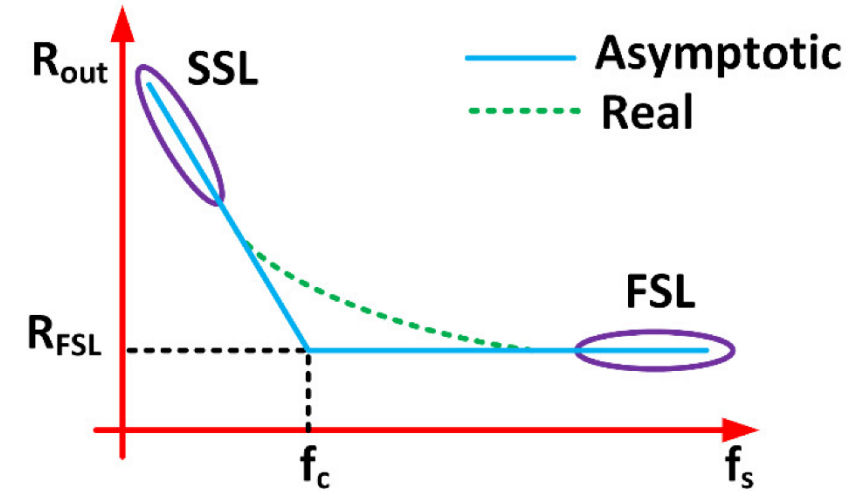
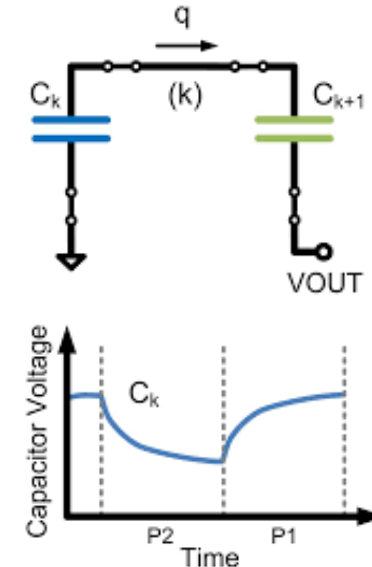
# Hybrid Switched-Capacitor-Magnetics Approach

## ➤ Energy Density of Capacitors vs. Inductors

- Capacitors are 100x denser than inductors
- Switched capacitor circuit suffers loss and regulation



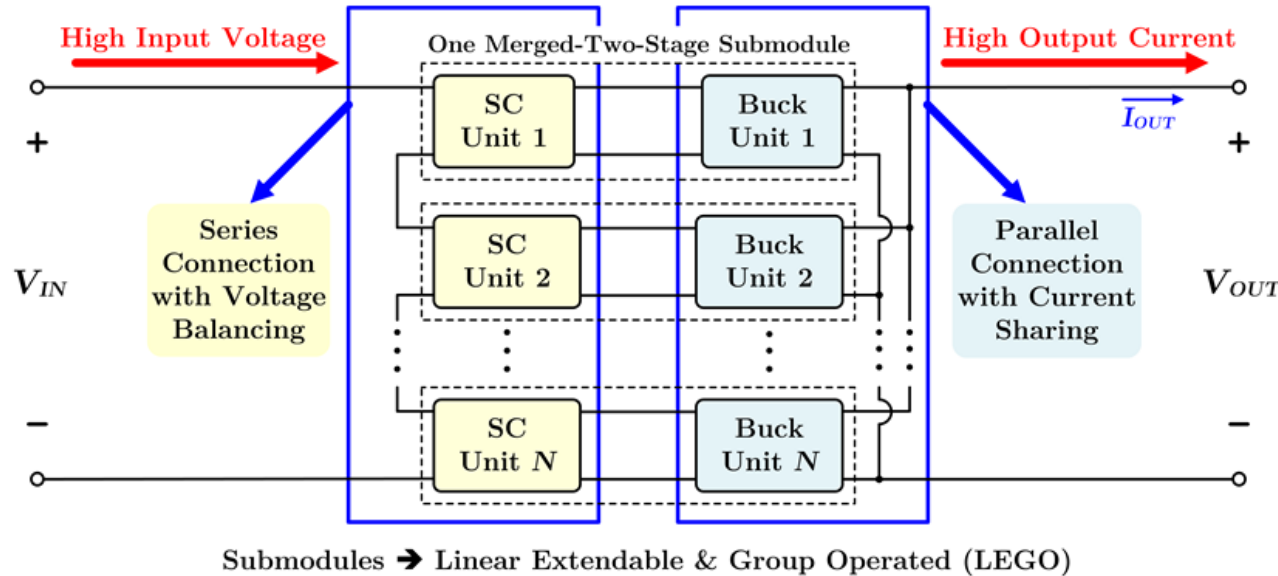
## ➤ Charge Sharing Loss of Switched Caps



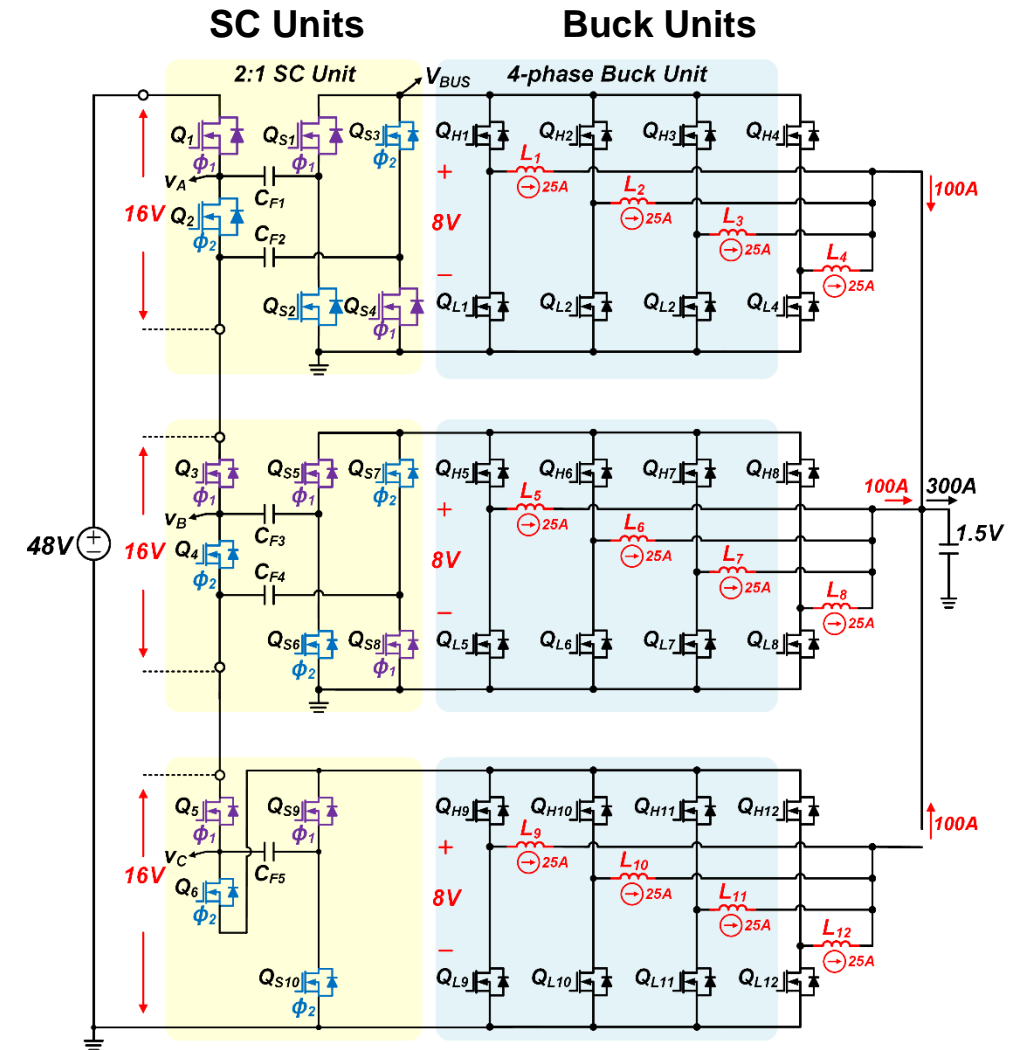
- Hybrid inductive and capacitive energy transfer**
- Capacitive energy transfer for power density
  - Inductive energy transfer for efficiency and regulation



# LEGO-PoL: Granular Building Block Approach for PoL



- Automatic current sharing
- Automatic voltage balancing
- Uniform thermal stress
- Capable of doing current mode control
- Fully modular and linear extendable



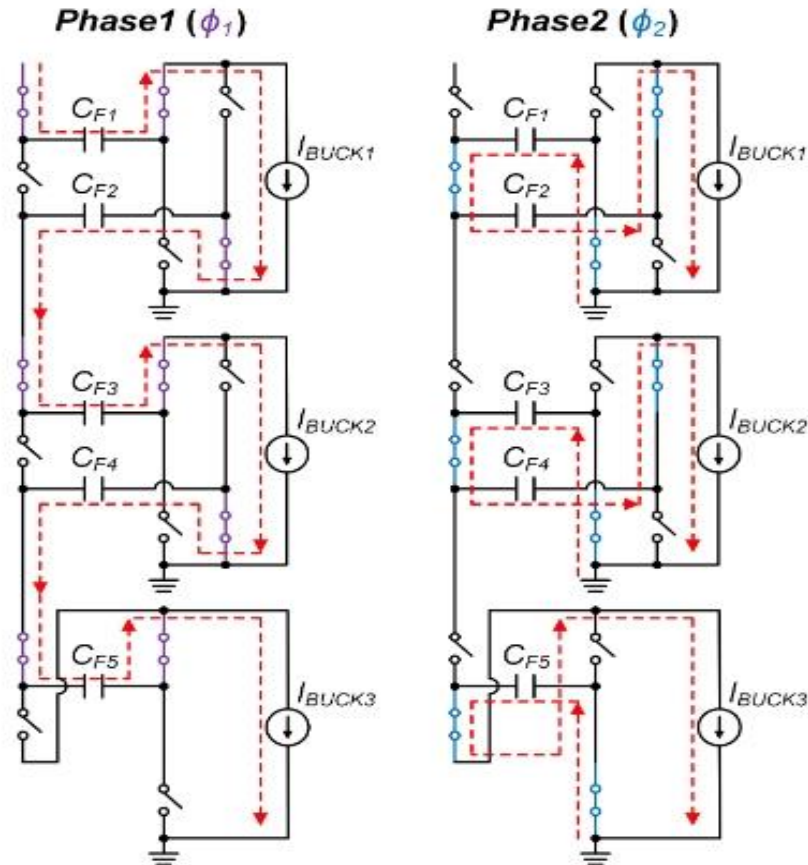
- J. Baek, Y. Elasser, and M. Chen, "3D LEGO-PoL: A 93.3% Efficient 48V-1.5V 450A Merged-Two-Stage Hybrid Switched-Capacitor Converter with 3D Vertical Coupled Inductors," APEC 2021.





➤ Soft-Charging Operation of SC Circuit

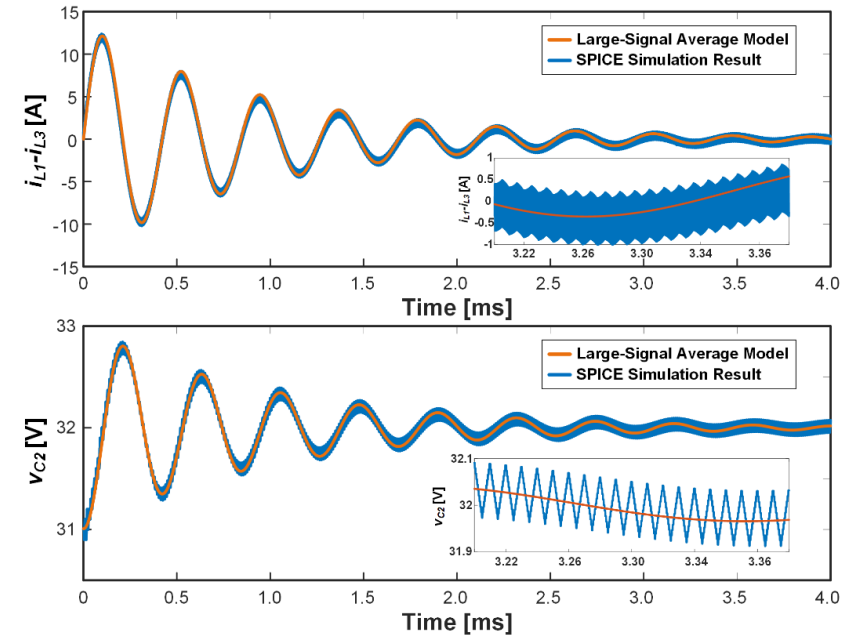
➤ Dynamics of Current Balancing



$$\ddot{\mathbf{X}} + \frac{R}{L}\dot{\mathbf{X}} + \frac{D^2}{ALC}M\mathbf{X} = 0,$$

$$\ddot{\mathbf{X}} = \begin{bmatrix} \frac{d^2 i_{L1}}{dt^2} \\ \frac{d^2 i_{L2}}{dt^2} \\ \vdots \\ \frac{d^2 i_{LN}}{dt^2} \end{bmatrix}, \quad \dot{\mathbf{X}} = \begin{bmatrix} \frac{di_{L1}}{dt} \\ \frac{di_{L2}}{dt} \\ \vdots \\ \frac{di_{LN}}{dt} \end{bmatrix}, \quad \mathbf{X} = \begin{bmatrix} i_{L1} \\ \vdots \\ i_{LN} \end{bmatrix},$$

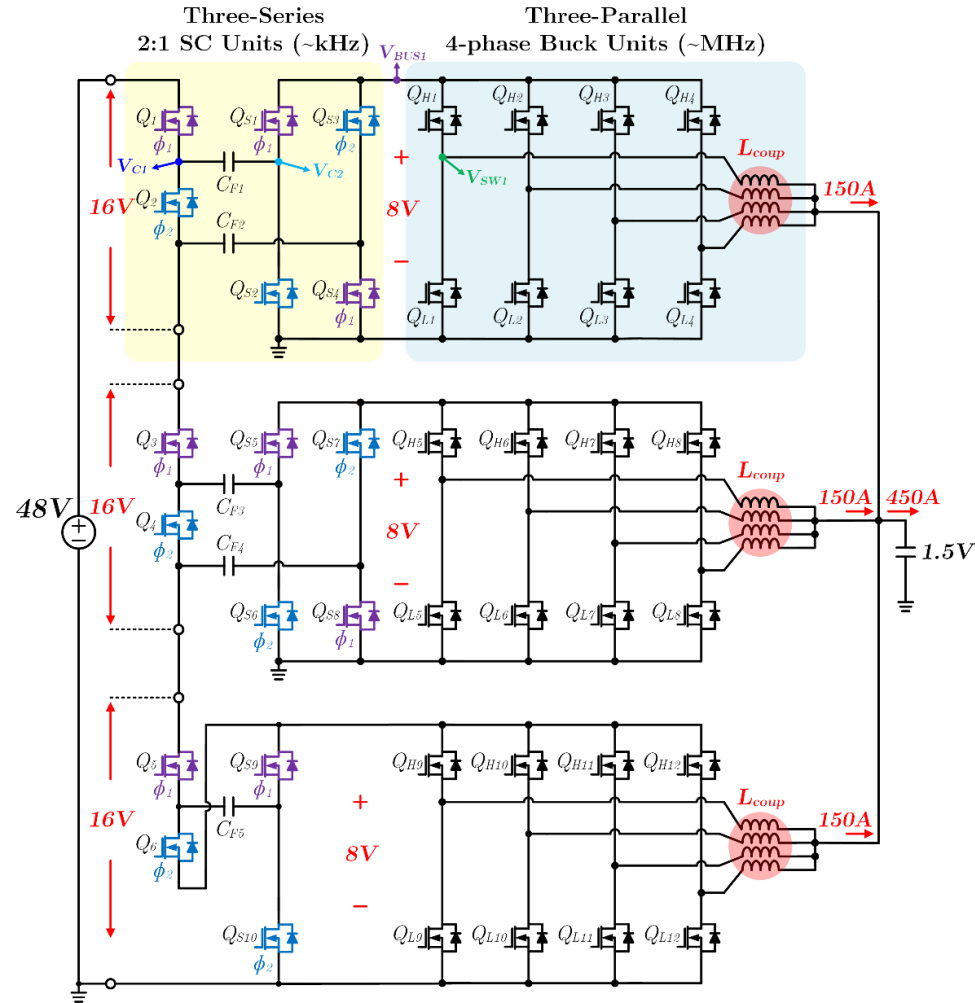
$$M = \begin{bmatrix} 1 & -1 & 0 & 0 & \dots & 0 \\ -1 & 2 & -1 & 0 & \dots & 0 \\ 0 & -1 & 2 & -1 & \dots & 0 \\ \vdots & \vdots & \vdots & \ddots & \dots & \vdots \\ 0 & 0 & \dots & -1 & 2 & -1 \\ 0 & 0 & \dots & 0 & -1 & 1 \end{bmatrix}.$$



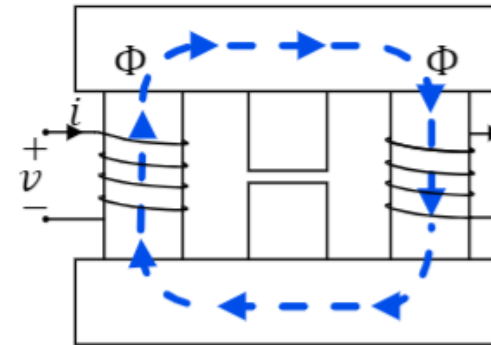
- Inductors soft-charge the switched capacitors
- Automatic current balancing of switched-capacitor circuits
- Low frequency voltage conversion & high frequency regulation



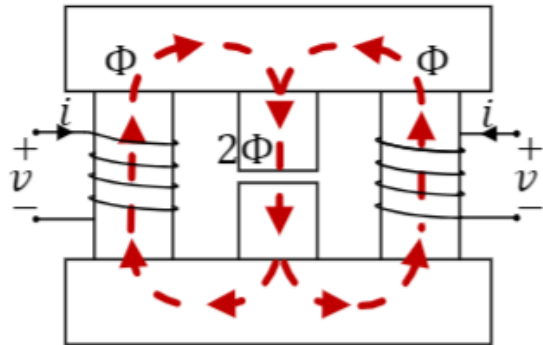
# Multiphase Coupled Inductor for Voltage Regulation



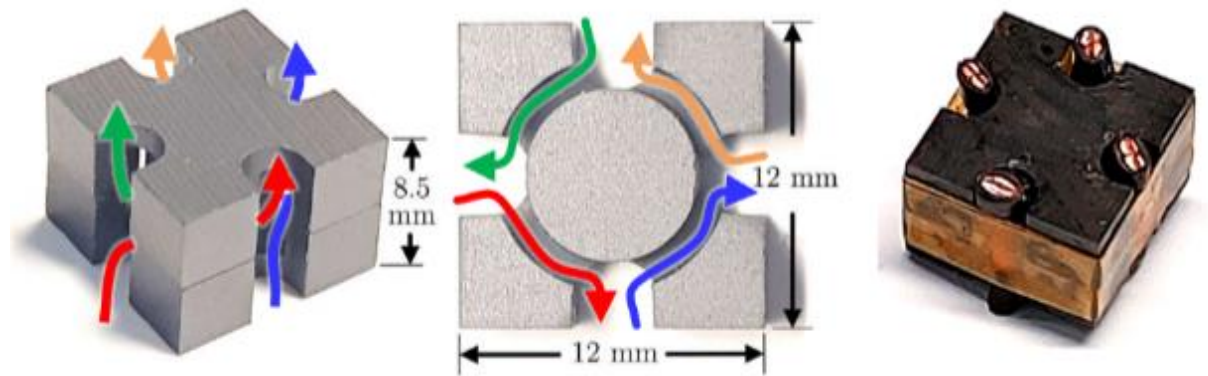
Differential Mode



Common Mode



Four Phase Vertical Coupled Inductor

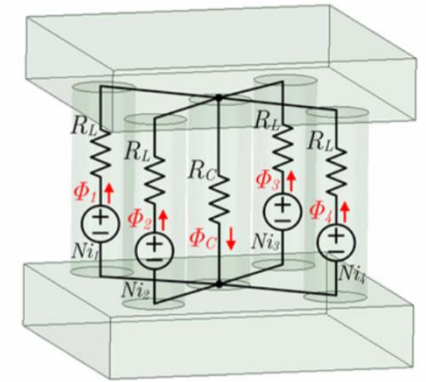
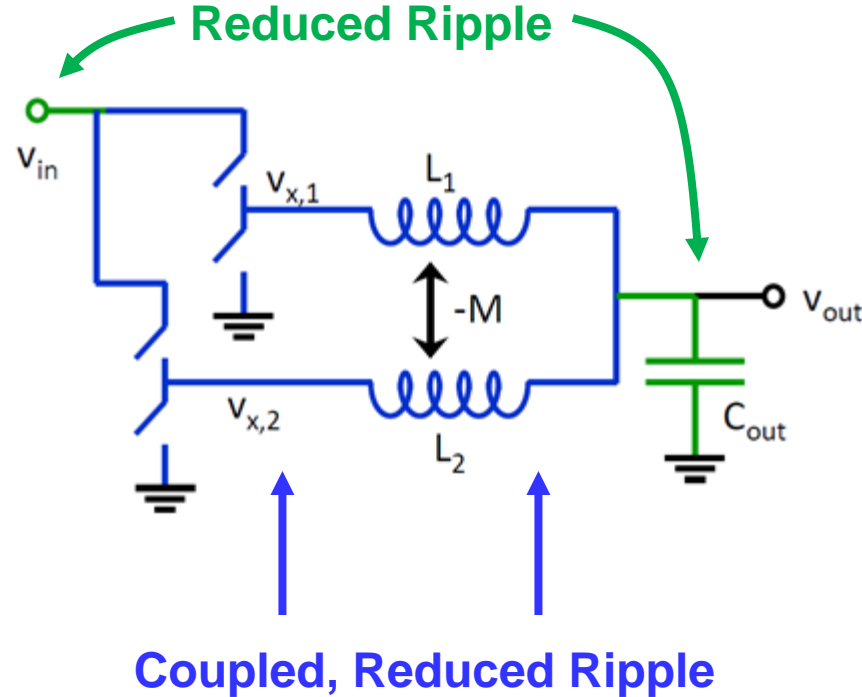
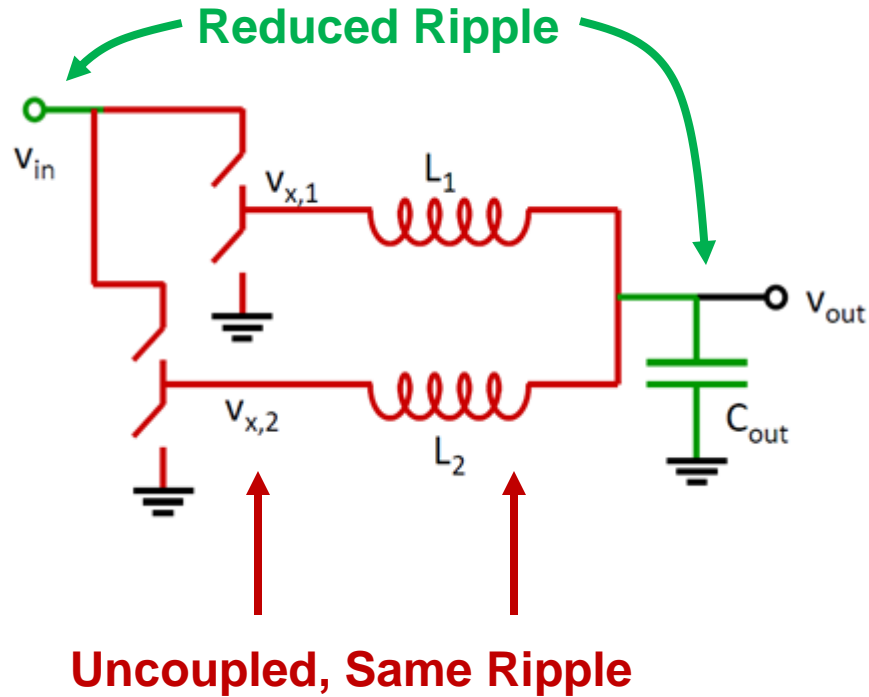


- J. Baek, Y. Elasser, and M. Chen, "3D LEGO-PoL: A 93.3% Efficient 48V-1.5V 450A Merged-Two-Stage Hybrid Switched-Capacitor Converter with 3D Vertical Coupled Inductors," APEC 2021.





# Unified Model for Multiphase Coupled Inductors



➤ Benefits of interleaving

$$\Gamma = \frac{(k + 1 - DM)(DM - k)}{(1 - D)DM^2}$$

➤ Coupling Coefficient

$$\beta = \frac{MR_C}{R_L}$$

➤ Benefits of Multiphase Coupling


$$\gamma = \frac{1 + \beta\Gamma}{1 + \beta}$$

- M. Chen and C. R. Sullivan, "Unified Models for Coupled Inductors Applied to Multiphase PWM Converters," IEEE Transactions on Power Electronics, accepted.



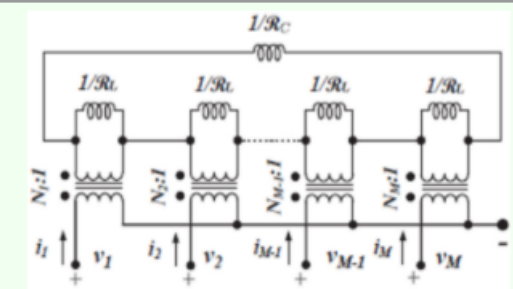
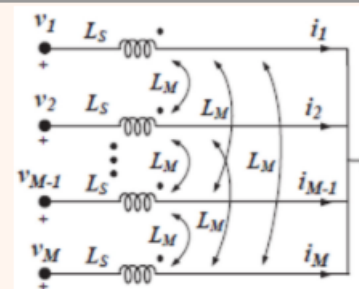
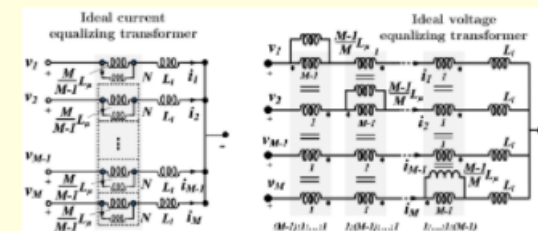
# Software Tool for Coupled Inductor Design

Princeton Coupl



## Princeton Coupled Magnetics Design Tool

By Princeton Power Electronics Research Lab

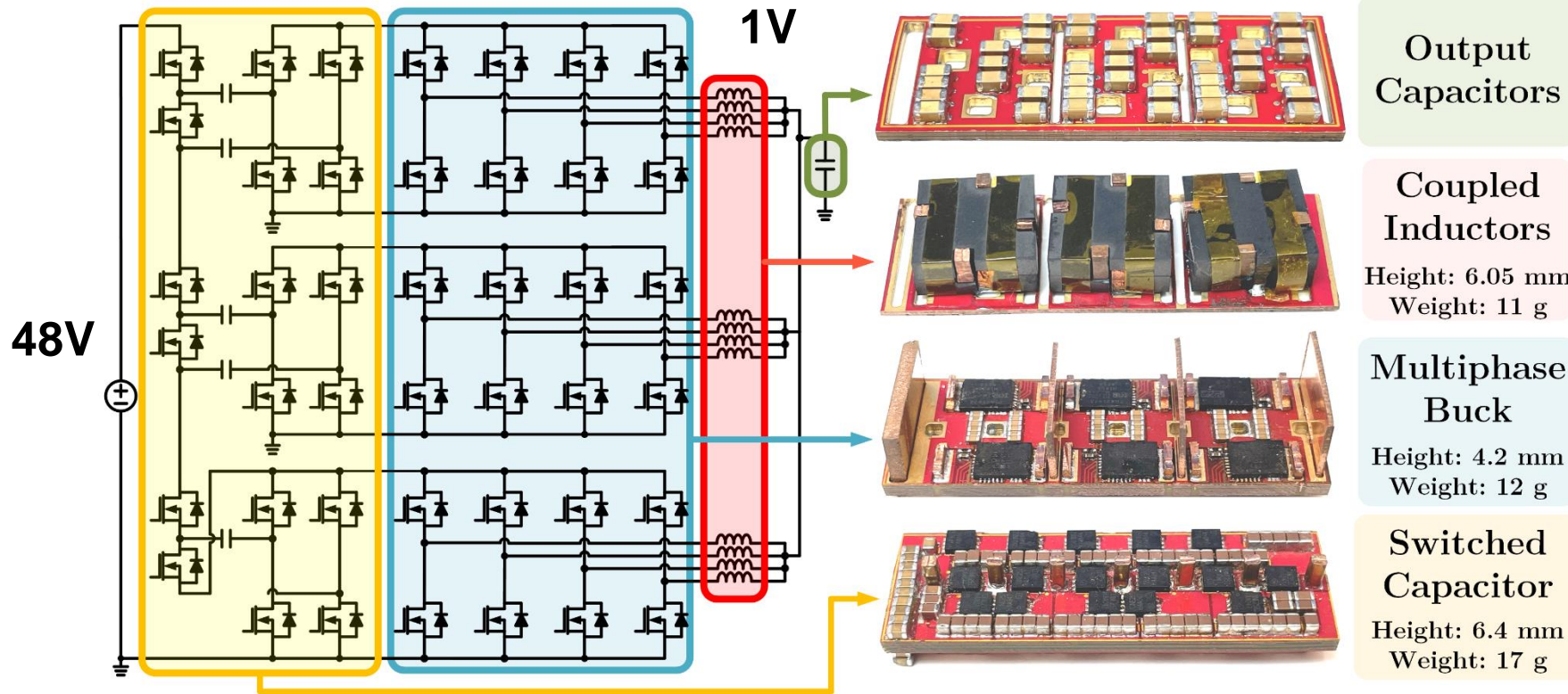
Input Parameters	Duty Ratio ( $D$ )	<input type="text"/>	Number of Phases ( $M$ )	<input type="text"/>	Number of Turns per Winding ( $N$ )	<input type="text"/>
Derived Parameters	Interleaving Boosting Inductance ( $1/\delta$ )	<input type="text"/>	Number of Overlapped Phases ( $k$ )	<input type="text"/>	Interleaving Ripple Compression ( $\delta$ )	<input type="text"/>
Method Name	Inductance Dual Model		Inductance Matrix Model		Multiwinding Transformer Model	
Design Parameters	$R_L$	<input type="text"/>	$L_S$	<input type="text"/>	$L_l$	<input type="text"/>
	$R_C$	<input type="text"/>	$L_M$	<input type="text"/>	$L_\mu$	<input type="text"/>
	$\beta = \frac{R_C}{R_L}$		$\alpha = \frac{L_M}{L_S}$		$\rho = \frac{L_\mu}{L_l}$	
Description Matrix	$N^2 \begin{bmatrix} \frac{d i_1}{d t} \\ \frac{d i_2}{d t} \\ \vdots \\ \frac{d i_M}{d t} \end{bmatrix} = \begin{bmatrix} R_L + R_C & R_C & \dots & R_C \\ R_C & R_L + R_C & \dots & R_C \\ \vdots & \vdots & \ddots & \vdots \\ R_C & \dots & R_C & R_L + R_C \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_M \end{bmatrix}$	$\begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_M \end{bmatrix} = \begin{bmatrix} L_S & L_M & \dots & L_M \\ L_M & L_S & \dots & L_M \\ \vdots & \vdots & \ddots & \vdots \\ L_M & \dots & L_M & L_S \end{bmatrix} \begin{bmatrix} \frac{d i_1}{d t} \\ \frac{d i_2}{d t} \\ \vdots \\ \frac{d i_M}{d t} \end{bmatrix}$	$\begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_M \end{bmatrix} = \begin{bmatrix} L_l + L_\mu & -\frac{1}{M-1} L_\mu & \dots & -\frac{1}{M-1} L_\mu \\ -\frac{1}{M-1} L_\mu & L_l + L_\mu & \dots & -\frac{1}{M-1} L_\mu \\ \vdots & \vdots & \ddots & \vdots \\ -\frac{1}{M-1} L_\mu & -\frac{1}{M-1} L_\mu & \dots & L_l + L_\mu \end{bmatrix} \begin{bmatrix} \frac{d i_1}{d t} \\ \frac{d i_2}{d t} \\ \vdots \\ \frac{d i_M}{d t} \end{bmatrix}$			
Lumped Circuit Model						



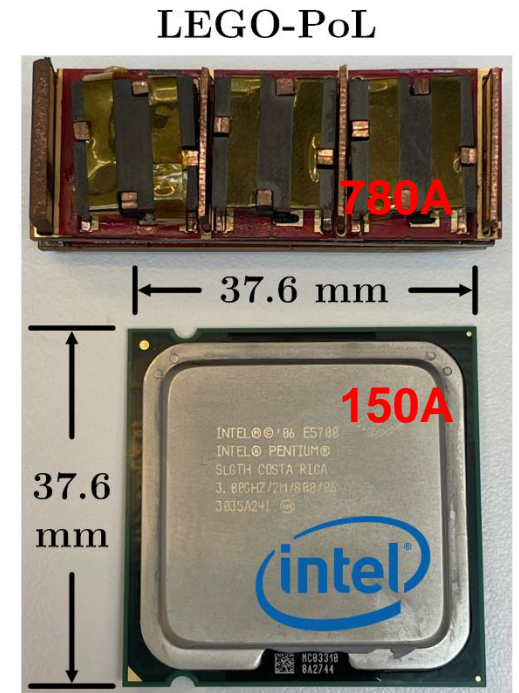
- M. Chen and C. R. Sullivan, "Unified Models for Coupled Inductors Applied to Multiphase PWM Converters," IEEE Transactions on Power Electronics, accepted.



# 3D Stacked Packaging for Vertical Power Delivery



- Output Capacitors
- Coupled Inductors  
Height: 6.05 mm  
Weight: 11 g
- Multiphase Buck  
Height: 4.2 mm  
Weight: 12 g
- Switched Capacitor  
Height: 6.4 mm  
Weight: 17 g

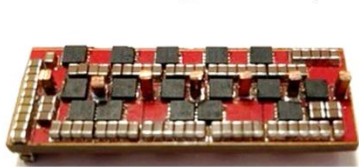


Switched Capacitor (SC)

SC + Buck

Coupled Inductors

SC + Buck + Inductors



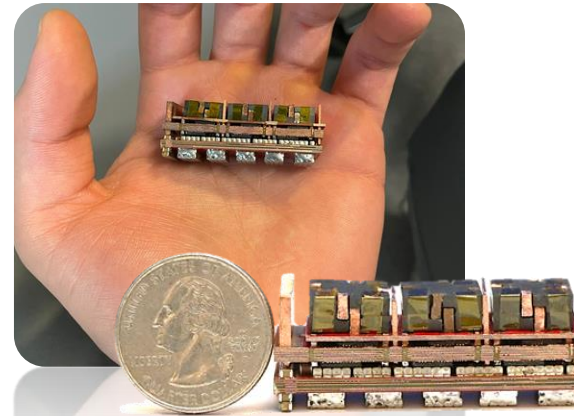
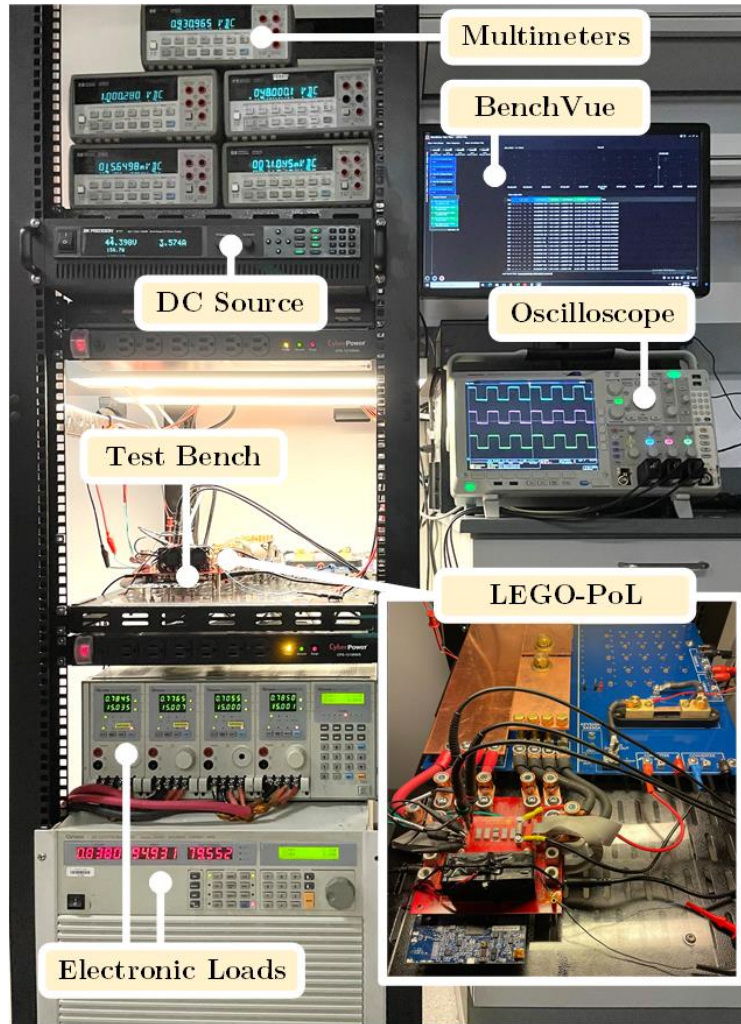
46.5 mm × 16.5 mm × 16.65 mm



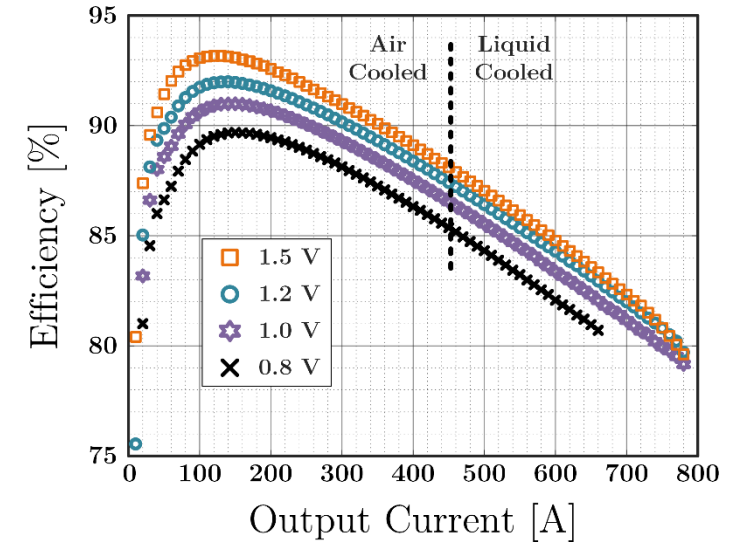
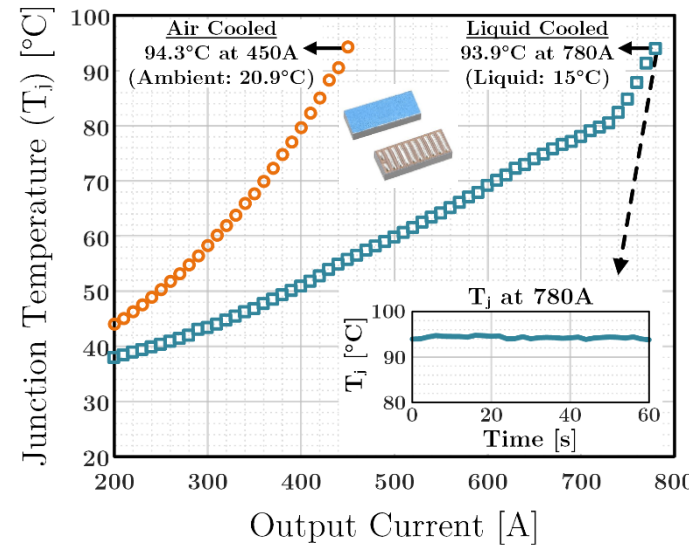
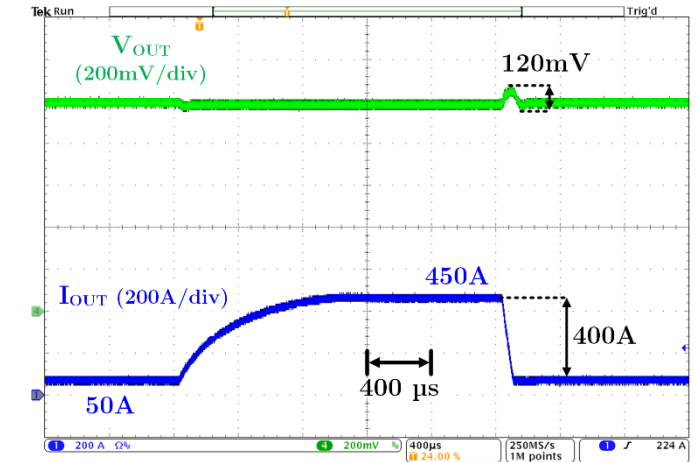
- J. Beak et al., "Vertical Stacked 48V-1V CPU Voltage Regulator with 91.1% Efficiency, 1 A/mm<sup>2</sup> Current Density and 1,000 W/in<sup>3</sup> Power Density", IEEE Transactions on Power Electronics, in preparation.



# Performance Summary

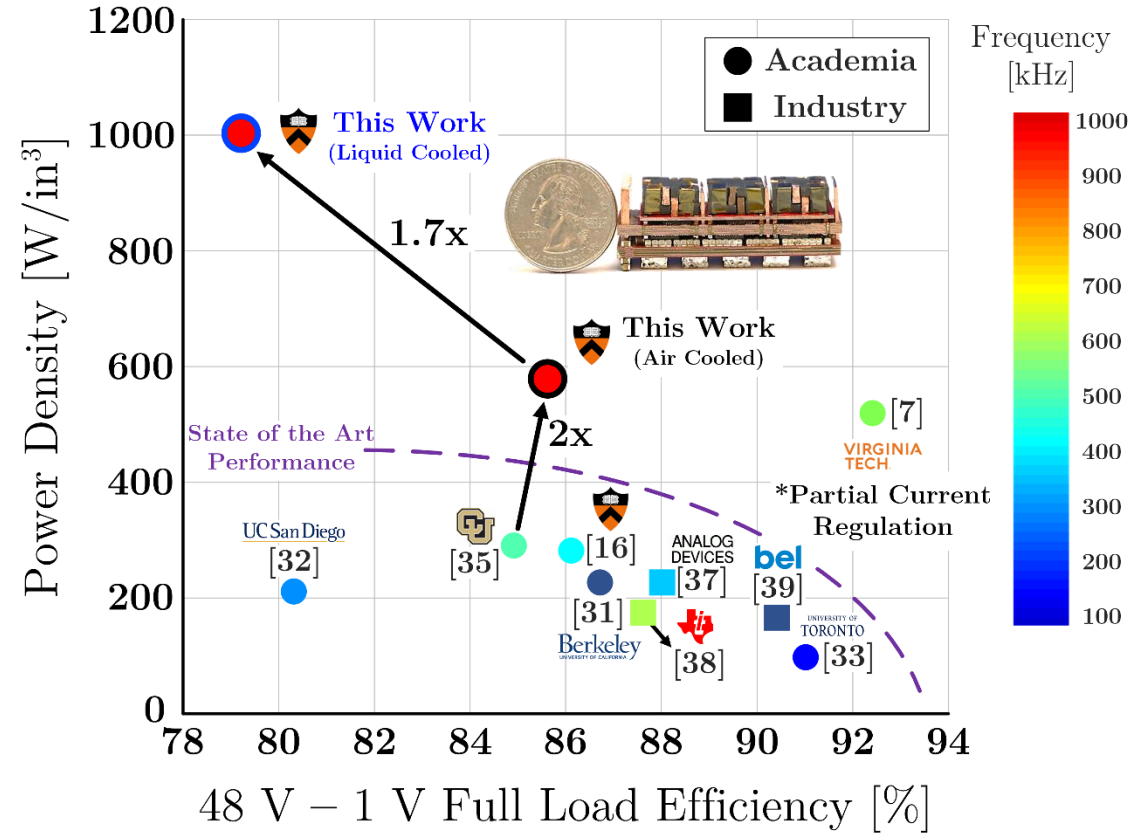
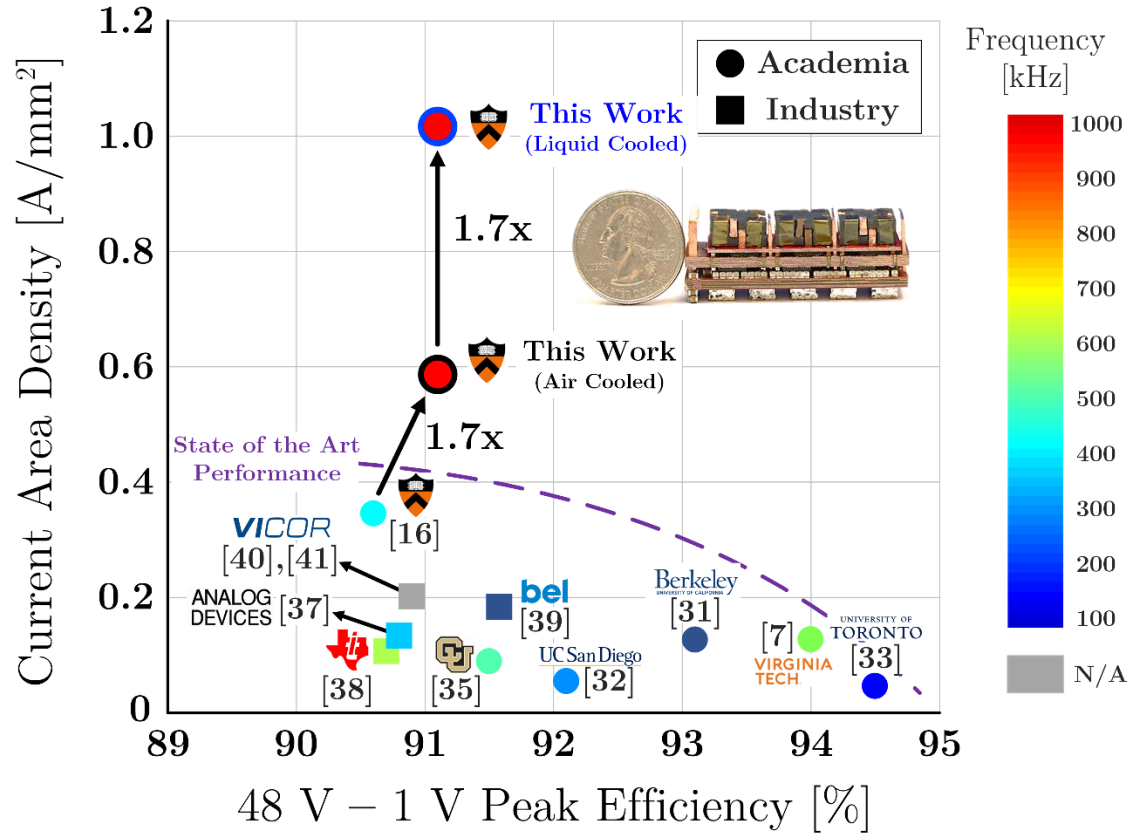


780 A, 1 V, 1 A/mm<sup>2</sup>, 1,000 W/in<sup>3</sup>



- J. Beak et al., “Vertical Stacked 48V-1V CPU Voltage Regulator with 91.1% Efficiency, 1 A/mm<sup>2</sup> Current Density and 1,000 W/in<sup>3</sup> Power Density”, IEEE Transactions on Power Electronics, in preparation.

# 780 A, 91.1% Peak Efficiency, 1000 W/in<sup>3</sup>, 1A/mm<sup>2</sup>



Sponsors & Collaborators:

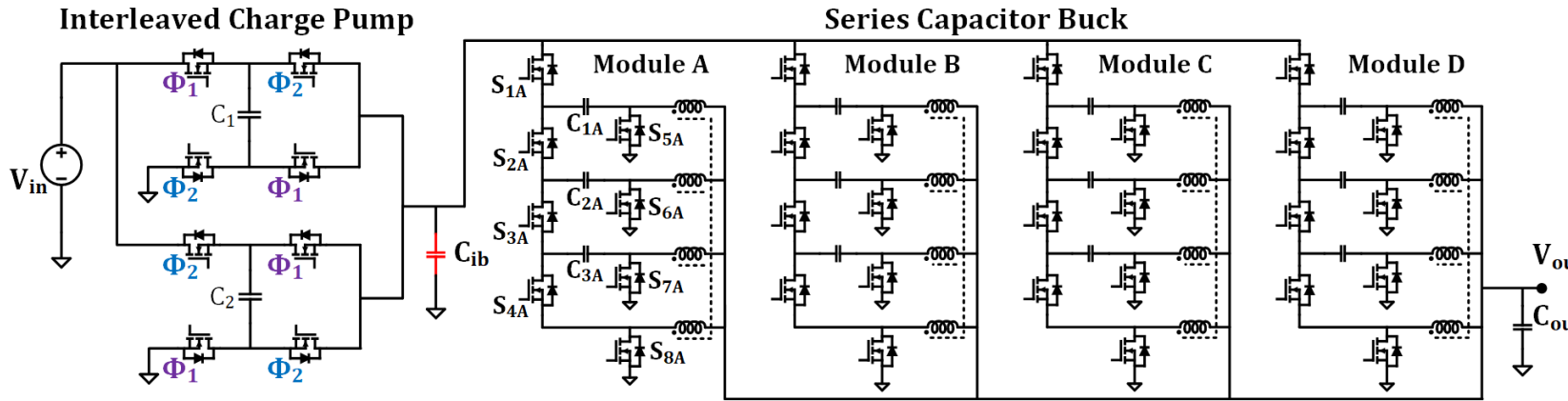


Dartmouth

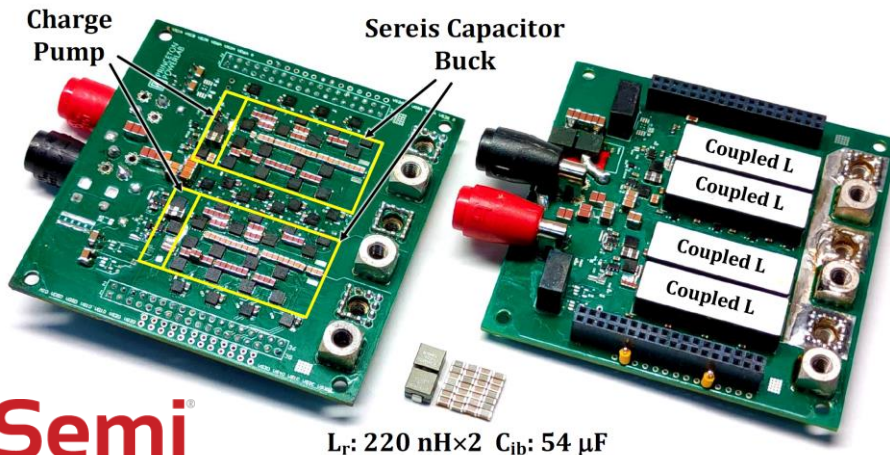
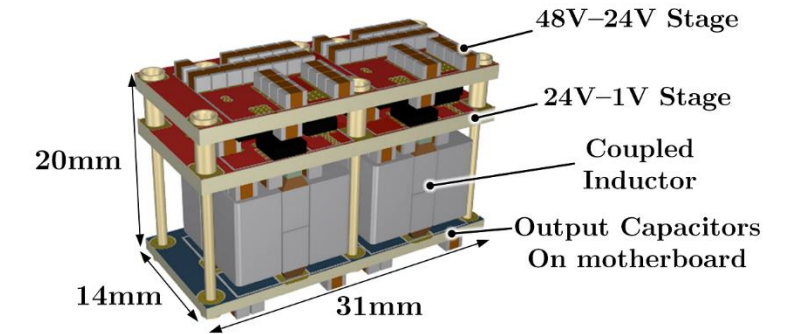
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# Alternative Designs for Extreme Efficiency



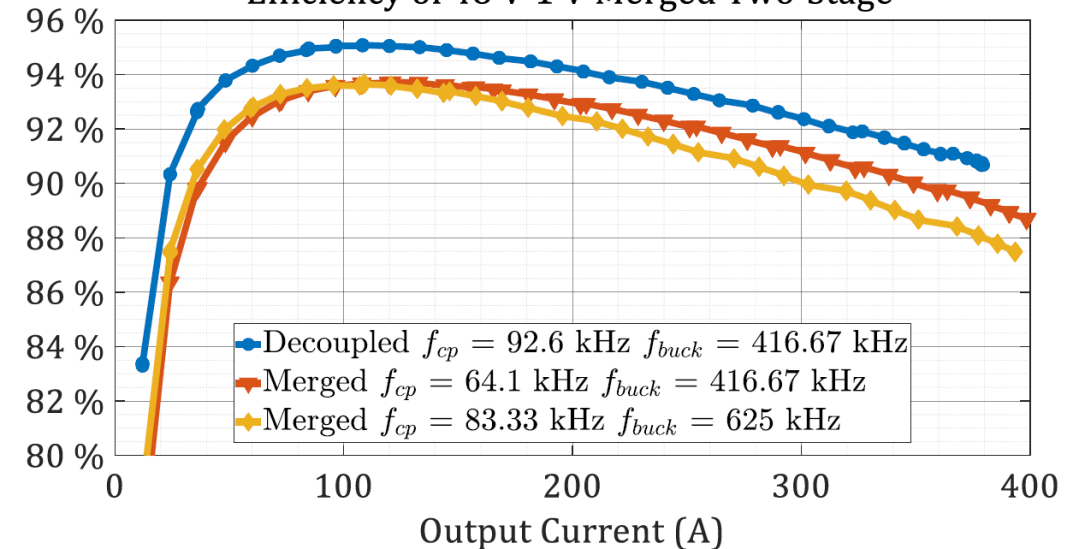
[Y. Chen COMPEL'20]



$L_r: 220 \text{ nH} \times 2$   $C_{ib}: 54 \mu\text{F}$

[Y. Chen APEC'21]

Efficiency of 48 V-1 V Merged Two-Stage

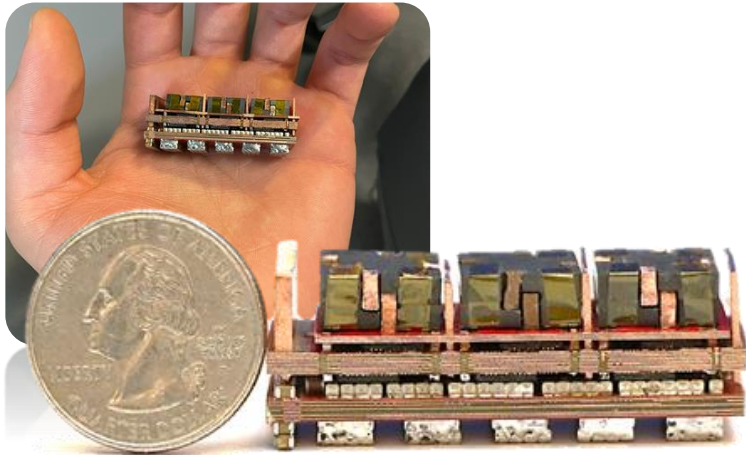


A GaN version to further shrink the size

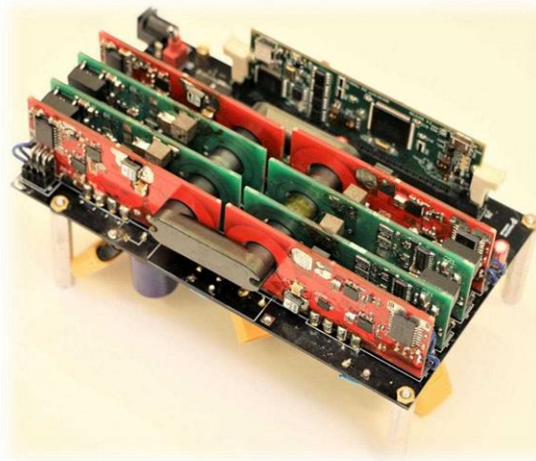
- Y. Chen, H. Cheng, D. Giuliano, M. Chen, "A 93.7% Efficient 400A 48V-1V Merged-Two-Stage Hybrid Switched-Capacitor Converter with 24V Virtual Intermediate Bus and Coupled Inductors," APEC 2021.



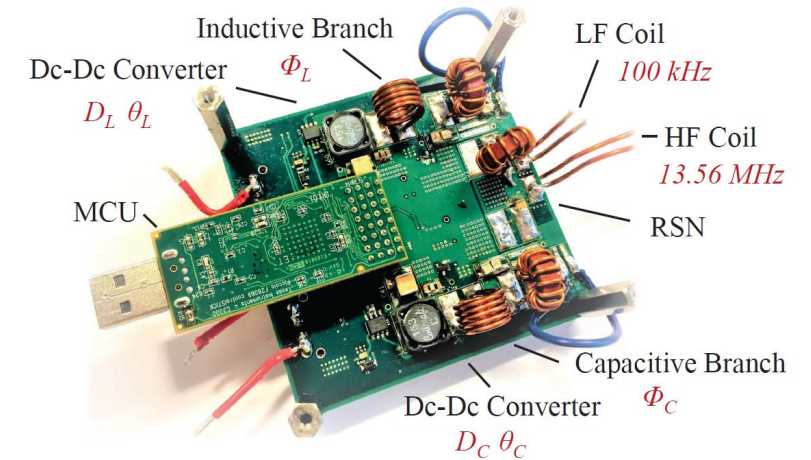
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*Compensate for Impedance Variation with Reactance Steering Network*



CPU Voltage Regulator



MIMO Energy Router



Dual-Band Wireless Power Transfer

# Large Scale Modular Energy Systems

Solar System



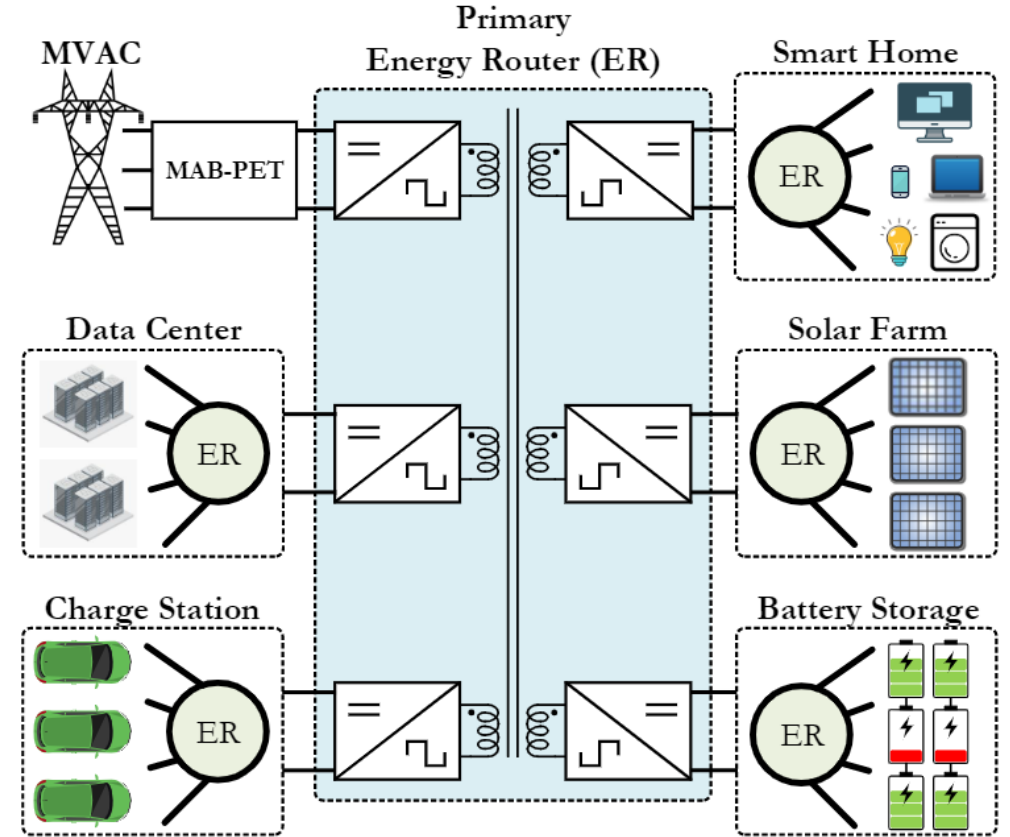
Battery System



Data Center Server



## MIMO Energy Router (ER) for Modular Loads



## Individual Converters



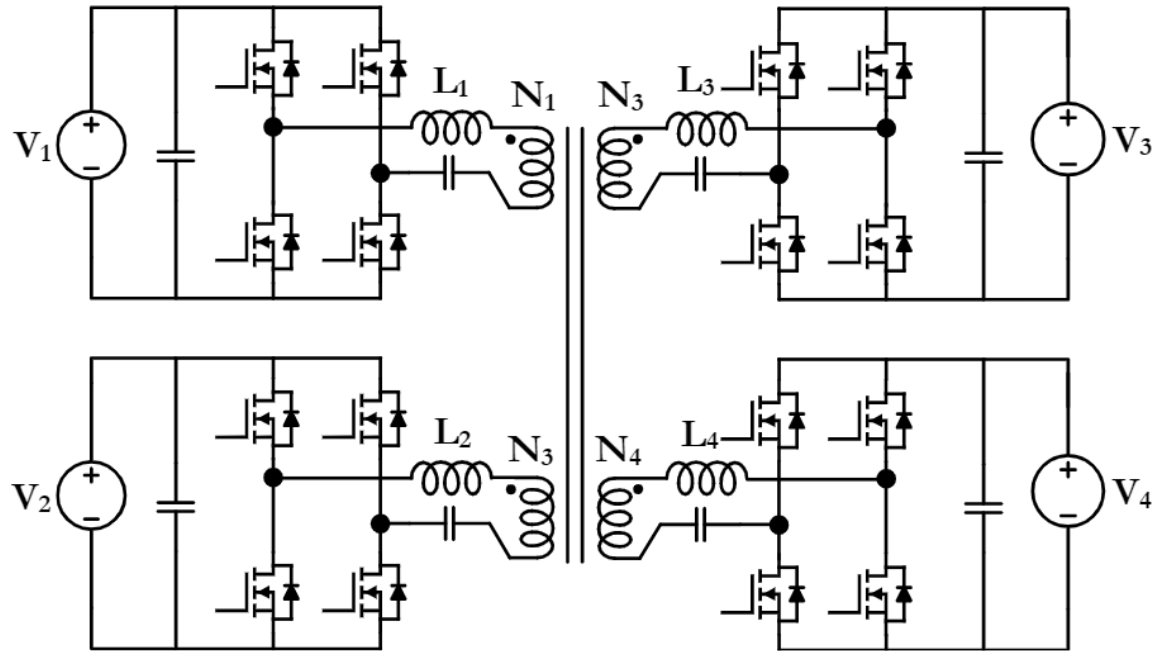
## MIMO Power Management



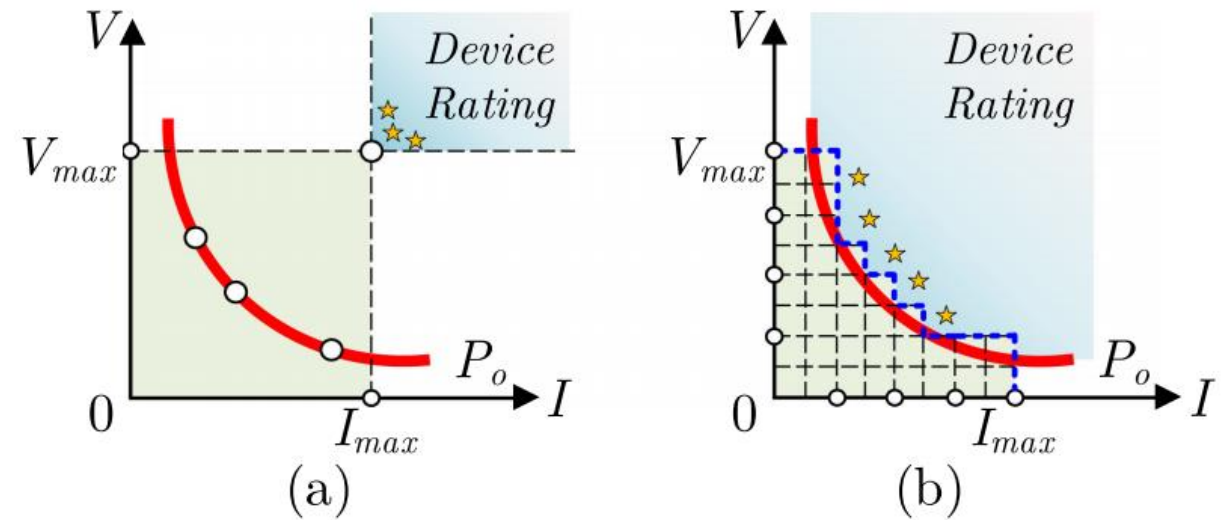
- Efficiency
- Density
- Weight
- Cost







## Flexible Programmable Granular Adaptive (FPGA)

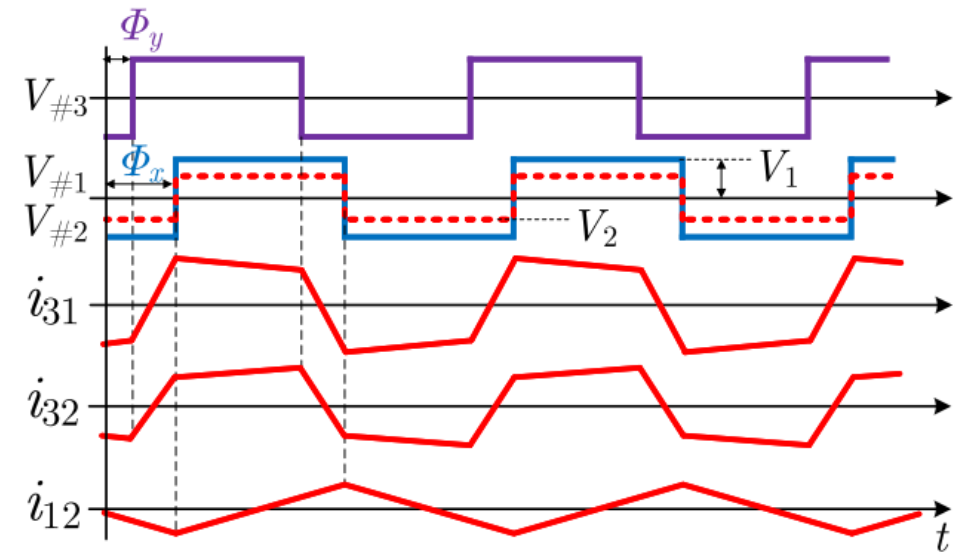
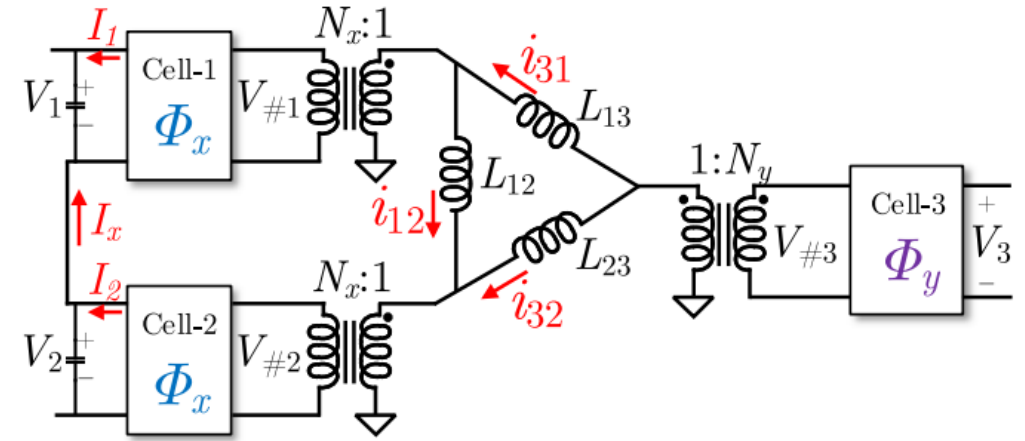
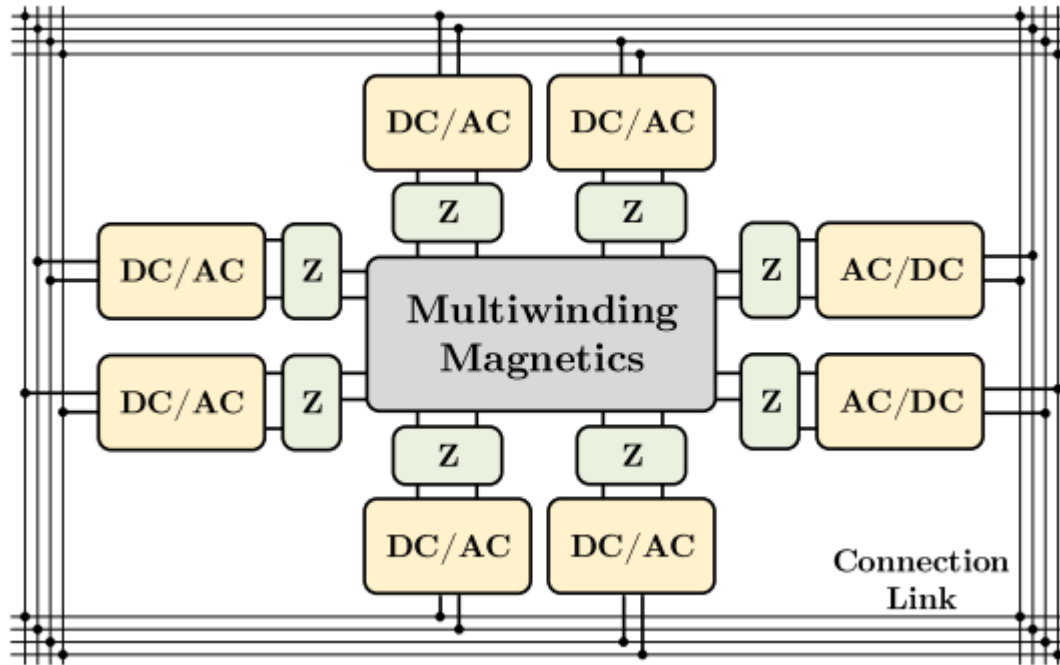


- MIMO power flow are highly dynamic
- Dynamically allocate power processing capability to different ports?

- Reconfiguration cells
- Sophisticated power flow
- Precise modeling and control



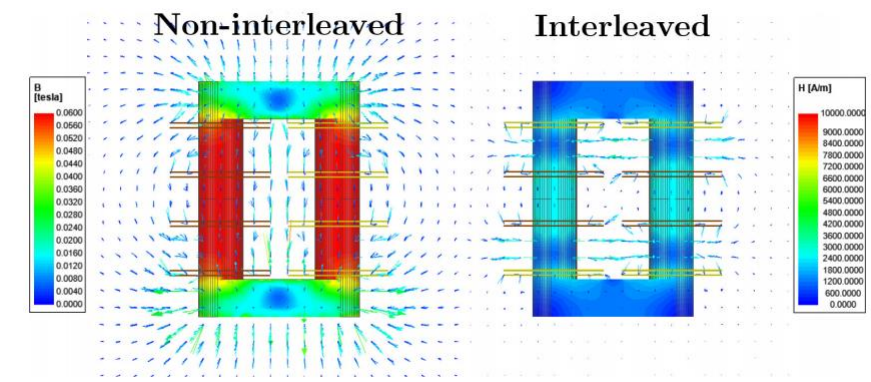
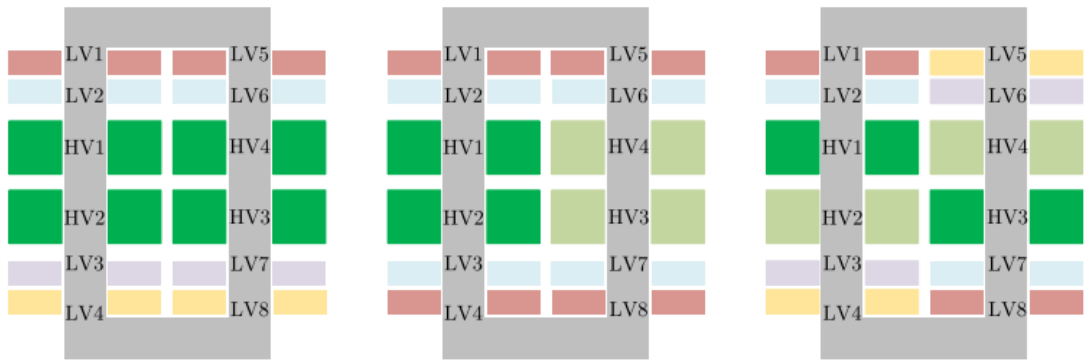
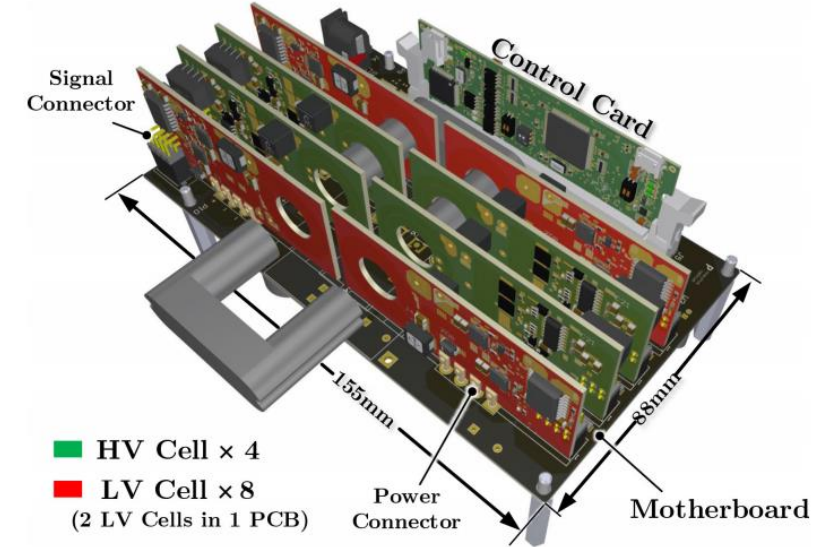
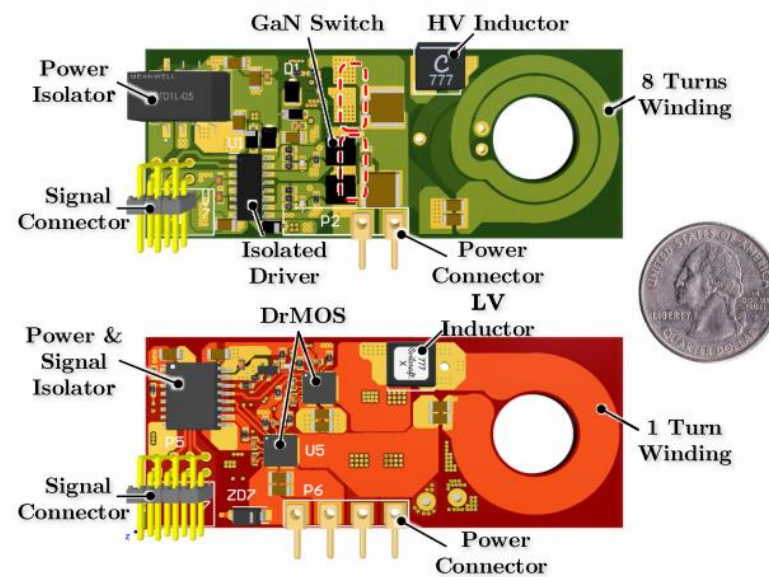
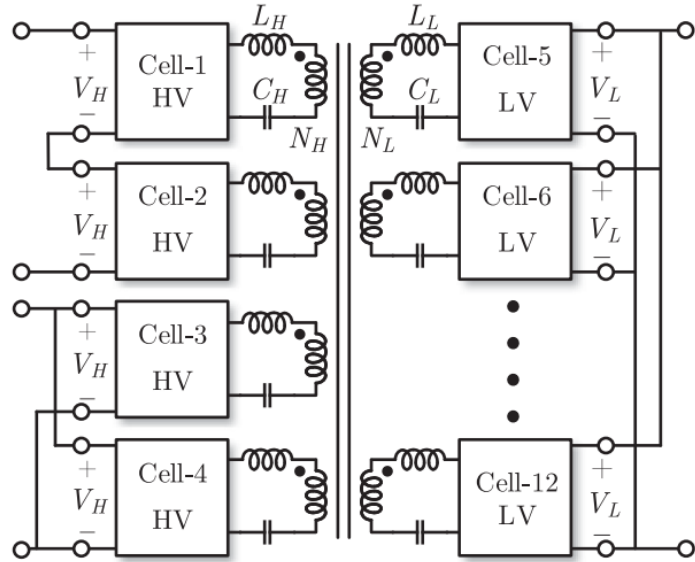
# Reconfigurable Multicell MIMO Energy Router



- Granular dc-ac building blocks as the “core”
- Magnetics as a central power processor “memory”
- Manage power in dc-domain instead of ac-domain
- Switch timing is important – WBG devices

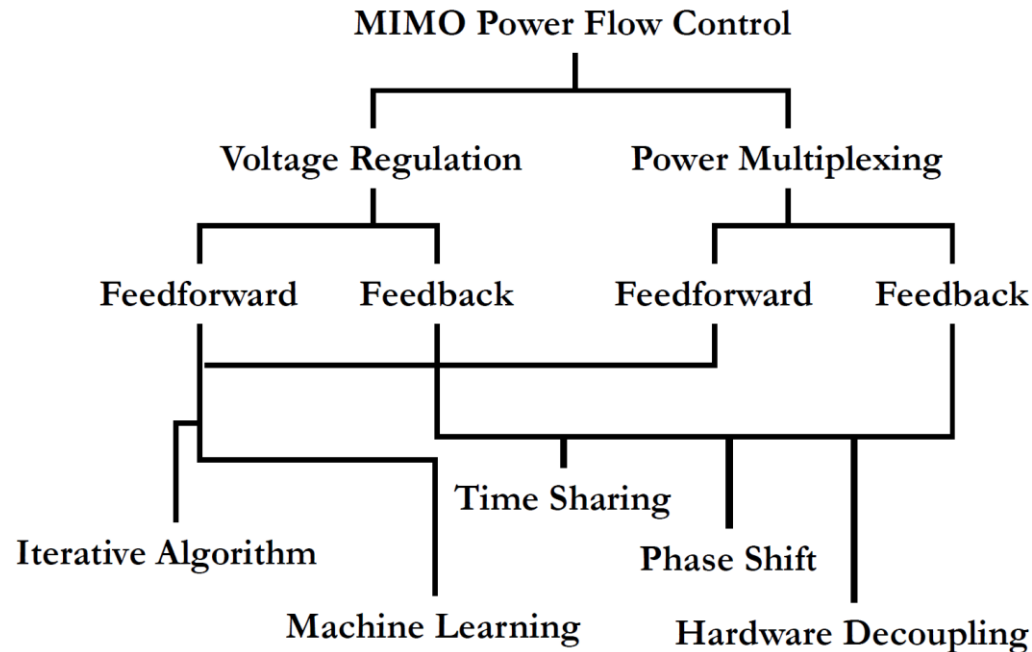


# Reconfigurable Multicell MIMO Energy Router

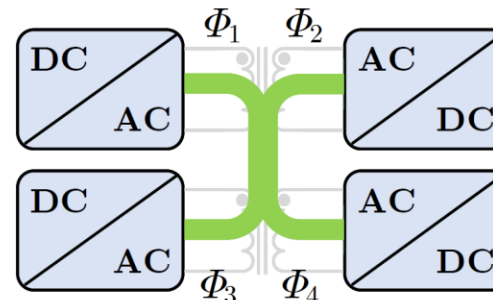


- Y. Chen, P. Wang, Y. Elasser, M. Chen, "Multicell Reconfigurable Multi-Input Multi-Output Energy Router Architecture," IEEE Transactions on Power Electronics, Dec. 2020.



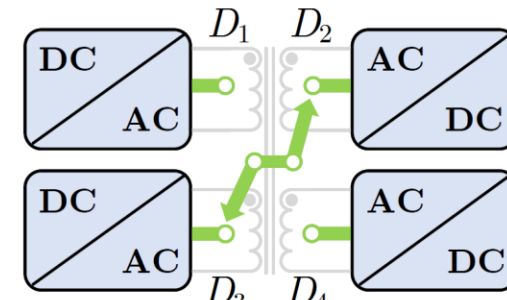


- **Phase-Shift**



- Partly decoupled
- High scalability
- High power throughput

- **Time-Sharing**



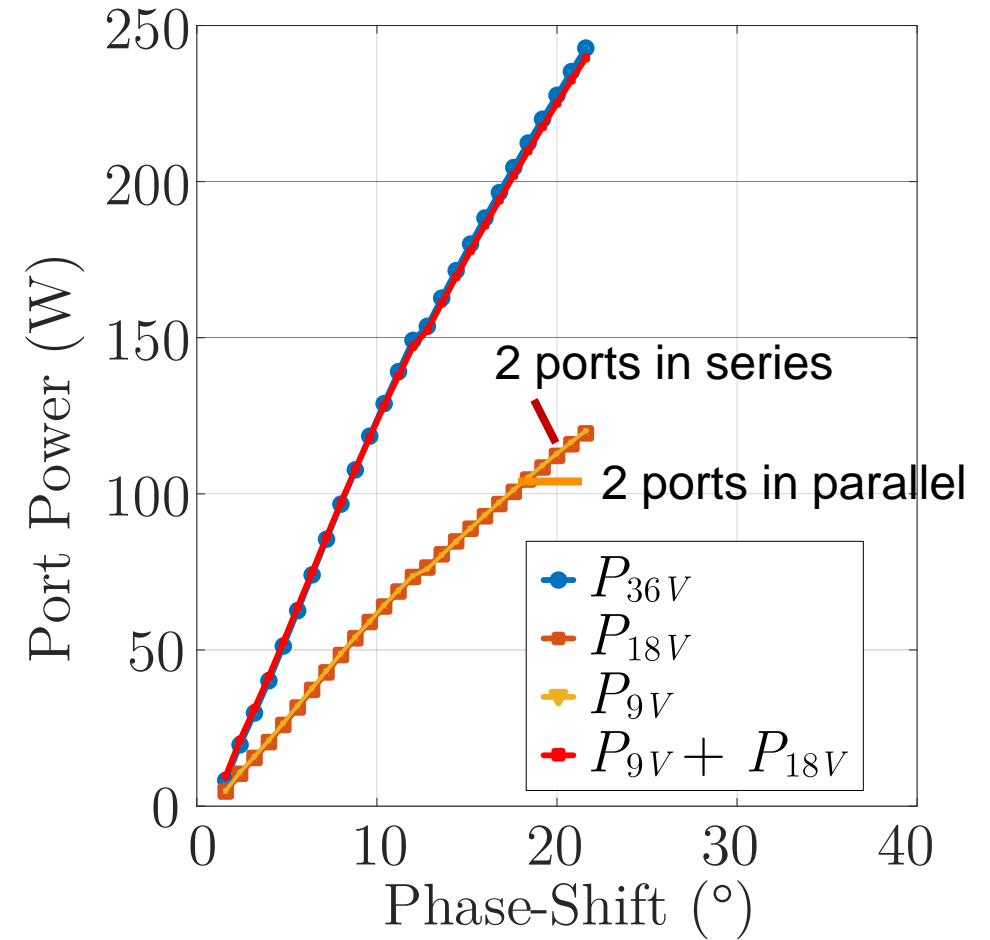
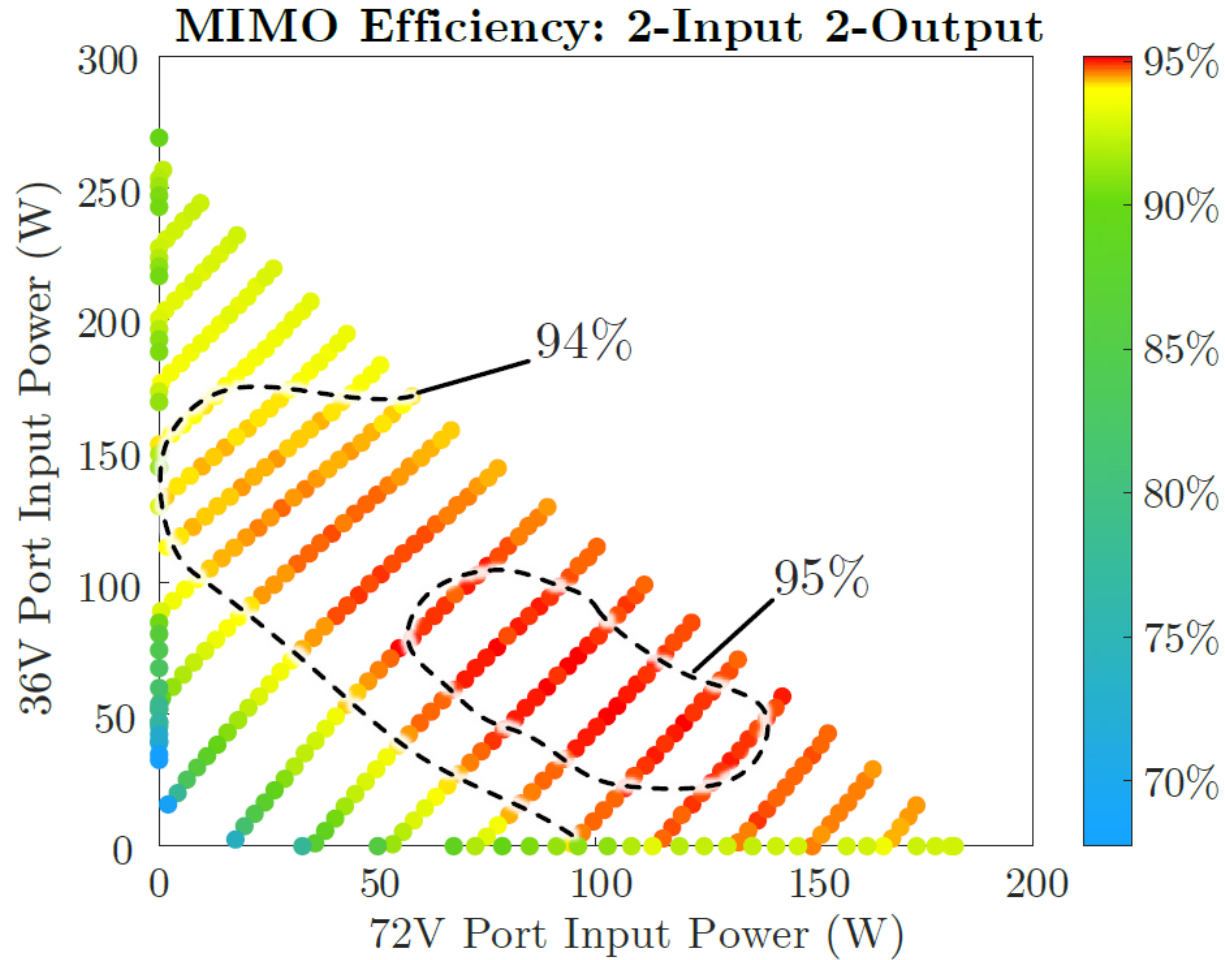
- Fully decoupled
- Limited scalability
- Limited power throughput

- P. Wang and M. Chen, "Towards Power FPGA: Architecture, Modeling and Control of Multiport Power Converters," IEEE 19th Workshop on Control and Modeling for Power Electronics (COMPEL), Padova, 2018, pp. 1-8.
- Y. Chen, P. Wang, H. Li and M. Chen, "Power Flow Control in Multi-Active-Bridge Converters: Theories and Applications," 2019 IEEE Applied Power Electronics Conference and Exposition (APEC), Anaheim, CA, USA, 2019, pp. 1500-1507.
- Bhattacharjee, A. K., Kutkut, N., and Batarseh, I. "Review of Multiport Converters for Solar and Energy Storage Integration," IEEE Transactions on Power Electronics, 2007, 34, (2), pp. 1431-1445.



- Y. Chen, P. Wang, Y. Elasser, M. Chen, "Multicell Reconfigurable Multi-Input Multi-Output Energy Router Architecture," IEEE Transactions on Power Electronics, Dec. 2020.

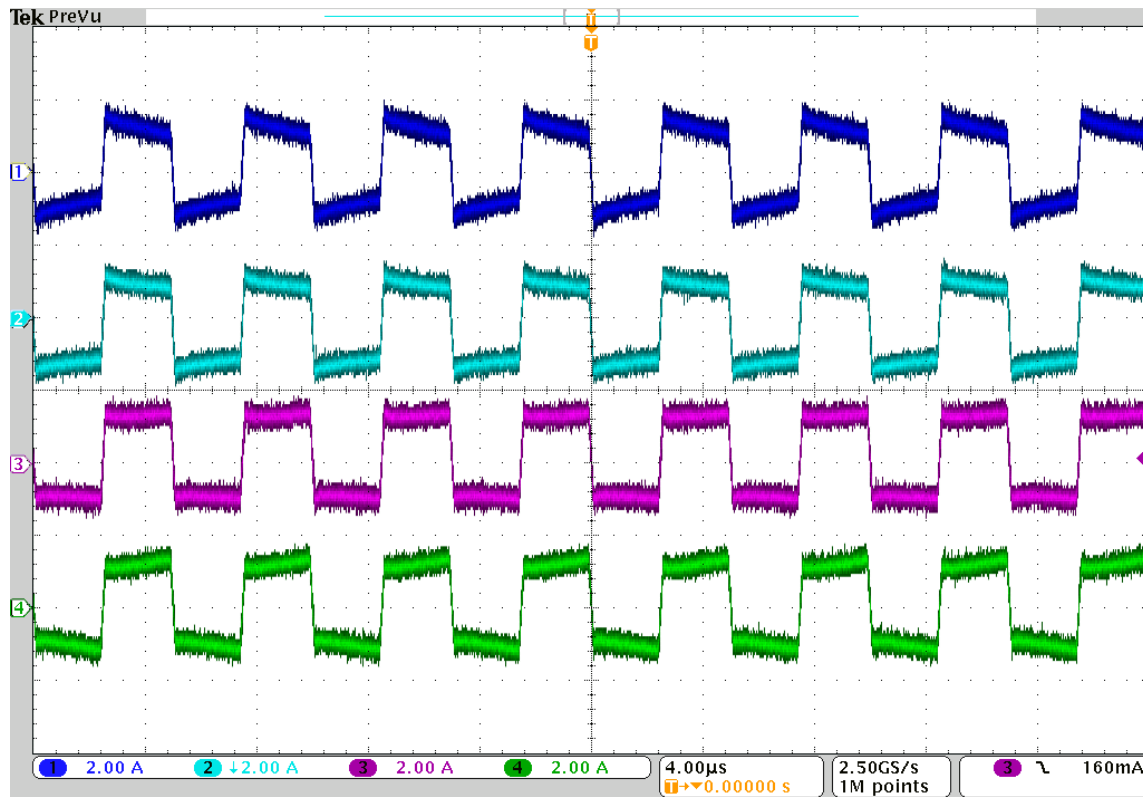
# Performance of the MIMO Energy Router



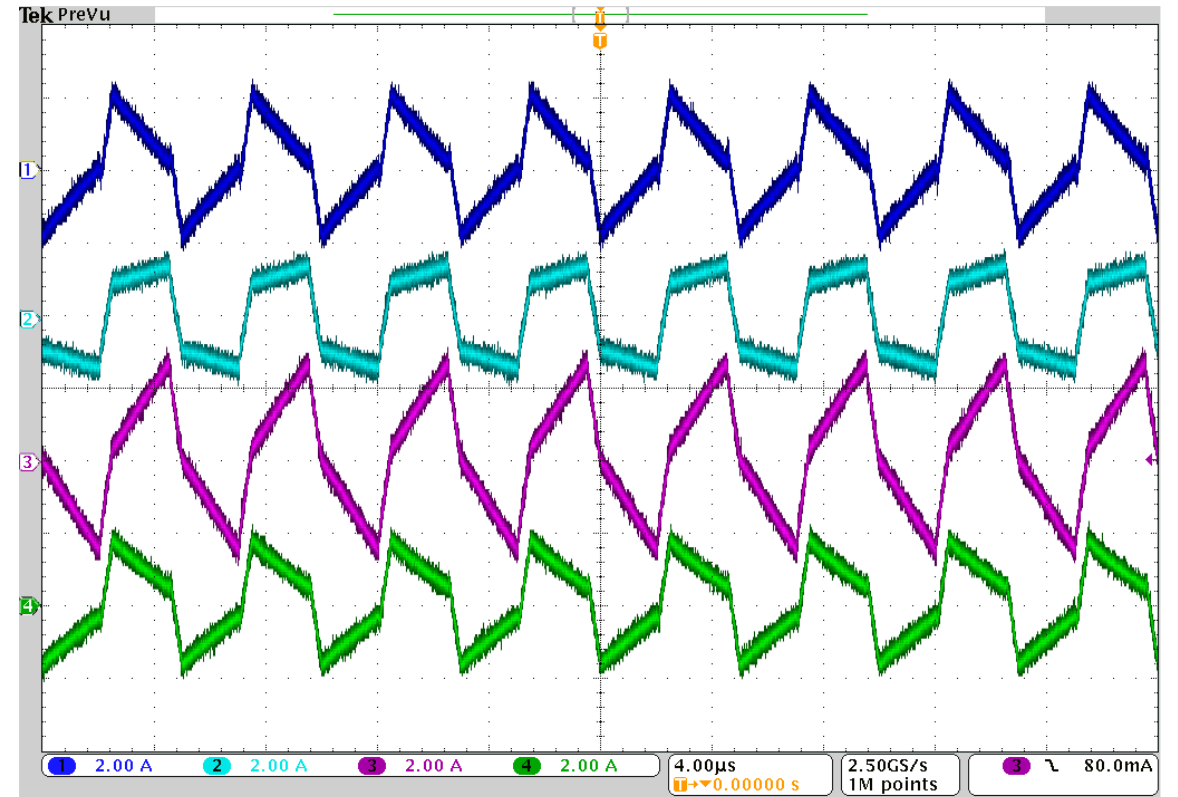
- Y. Chen, P. Wang, Y. Elasser, M. Chen, "Multicell Reconfigurable Multi-Input Multi-Output Energy Router Architecture," IEEE Transactions on Power Electronics, Dec. 2020.

# Operation Sensitive to Switch Timing

## Operating Condition #1



## Operating Condition #2

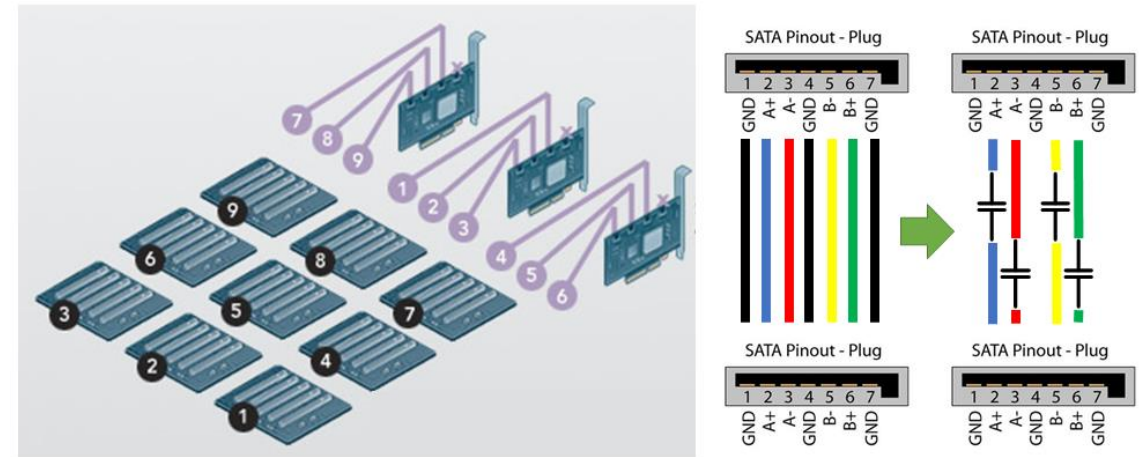
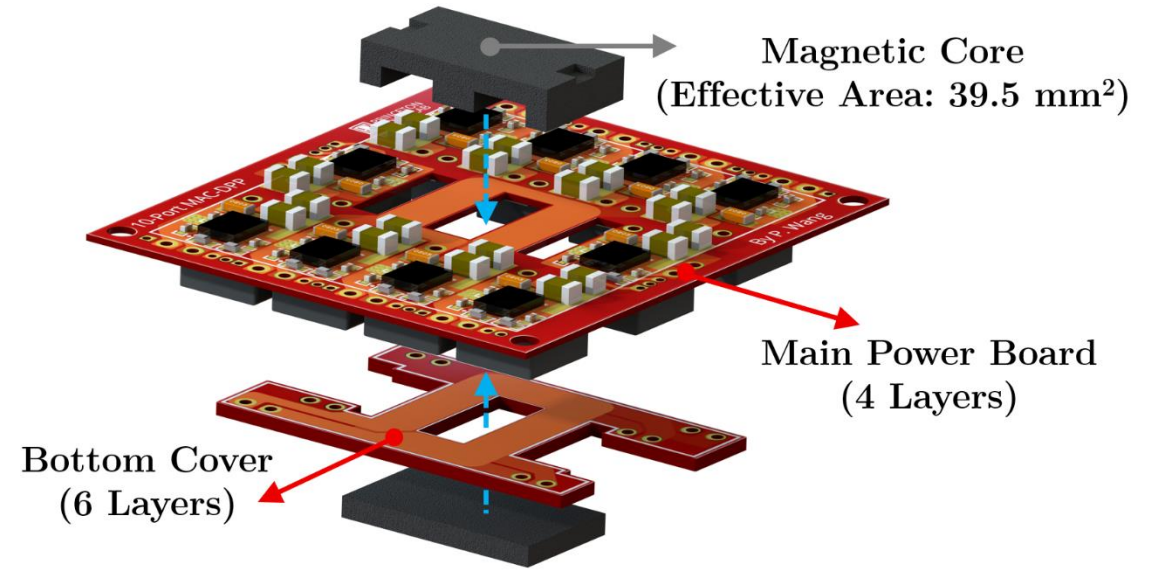
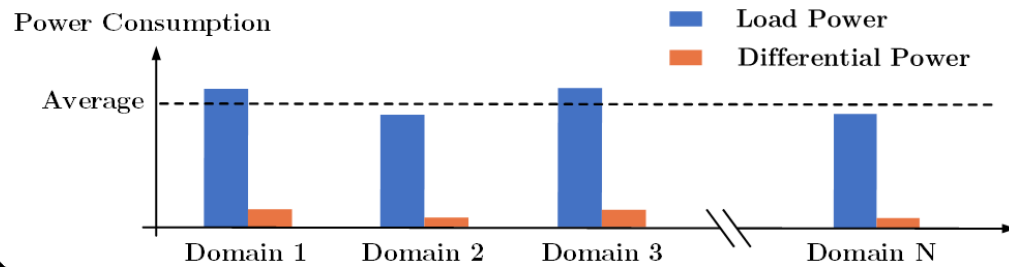
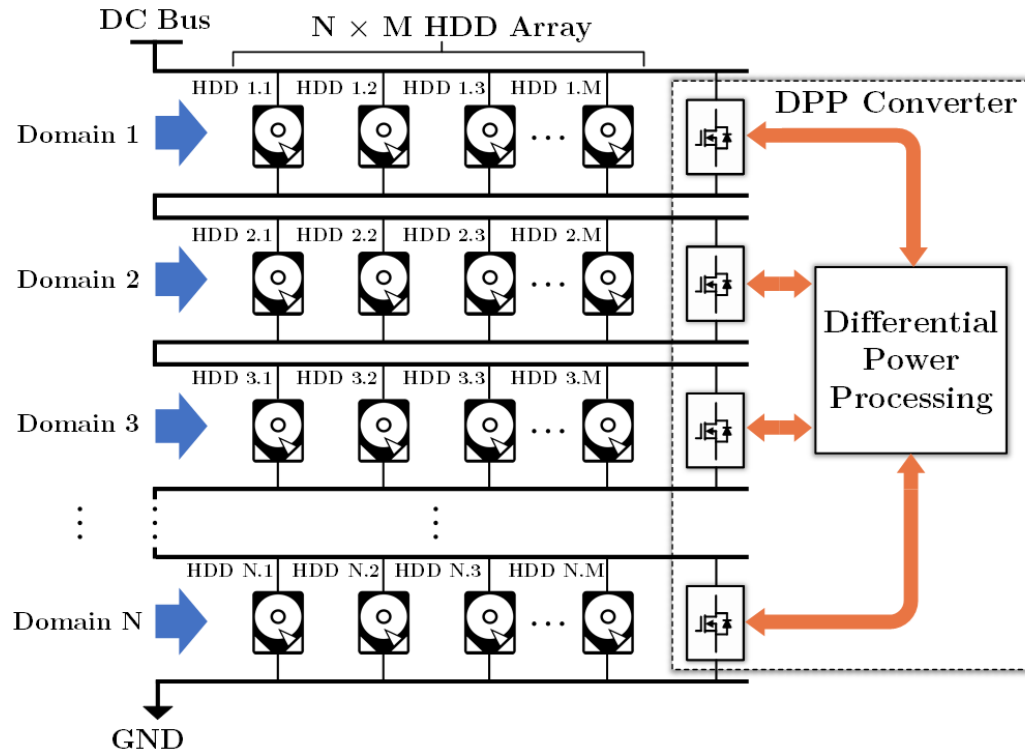


*Switching Frequency: 200 kHz*

- Y. Chen, P. Wang, Y. Elasser, M. Chen, "Multicell Reconfigurable Multi-Input Multi-Output Energy Router Architecture," IEEE Transactions on Power Electronics, Dec. 2020.

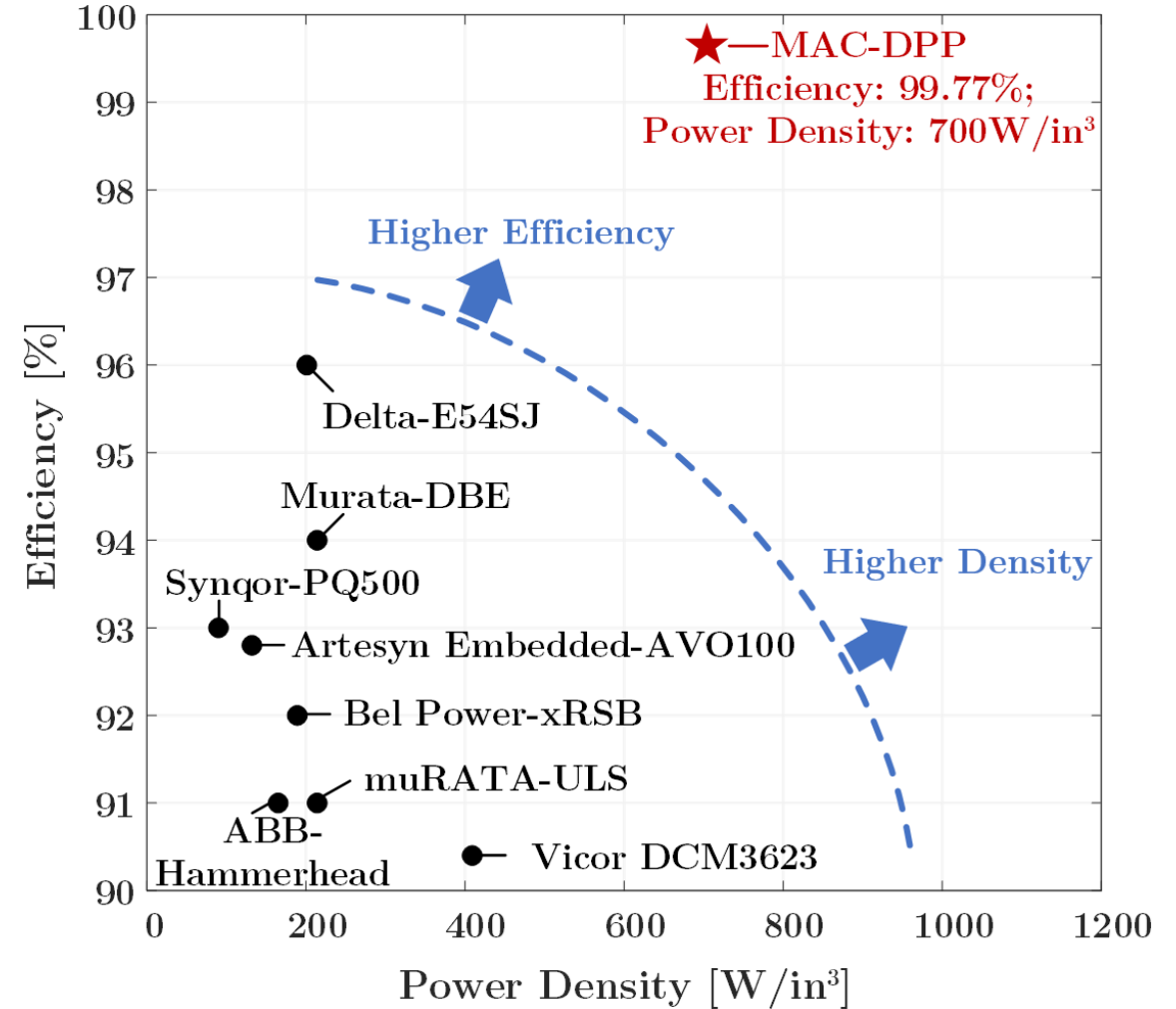
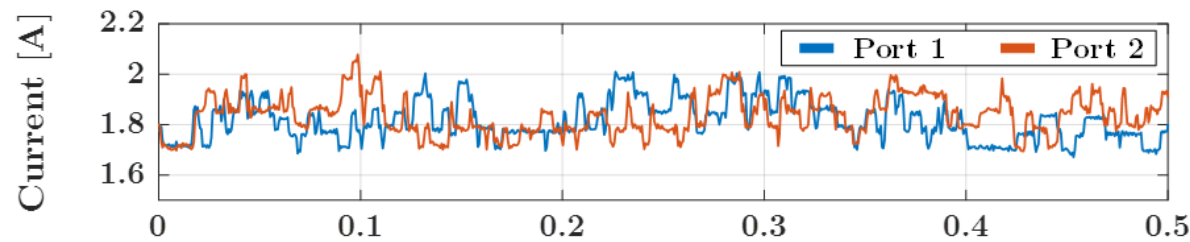
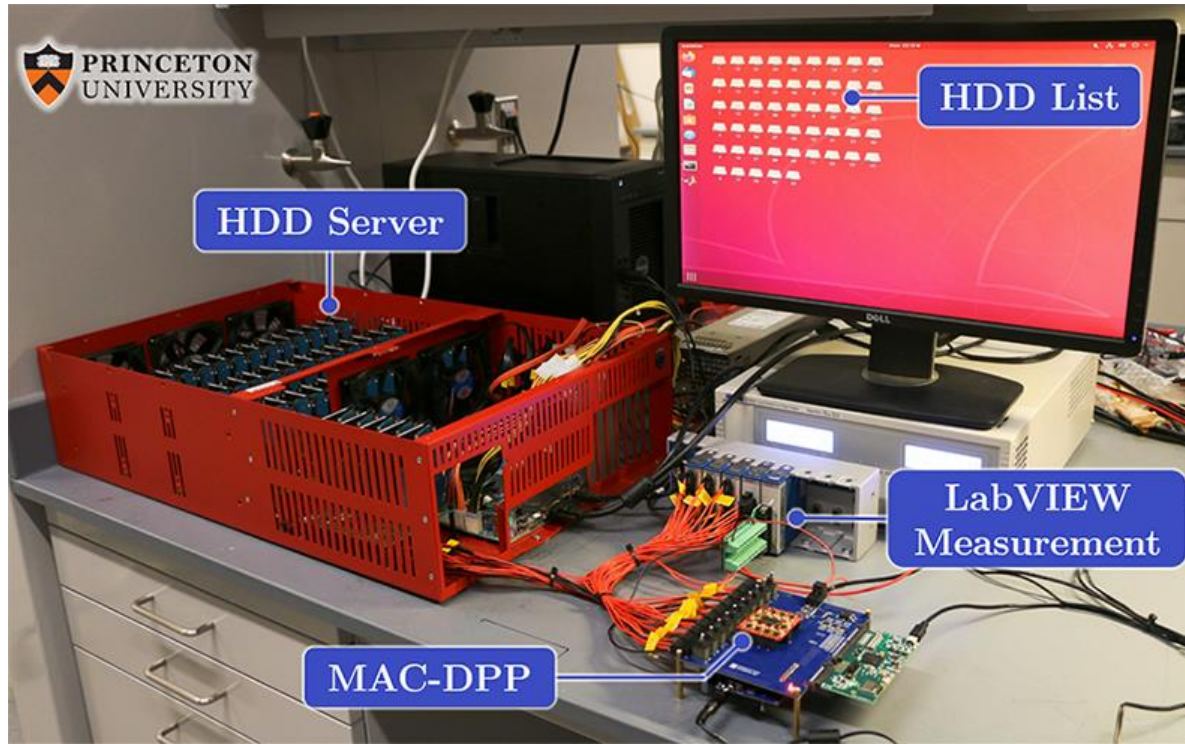


# Differential Power Processing for Data Storage



- P. Wang, Y. Chen, J. Yuan, R. C. N. Pilawa-Podgurski, M. Chen, "Differential Power Processing for Ultra-Efficient Data Storage," IEEE Transactions on Power Electronics, April 2021.

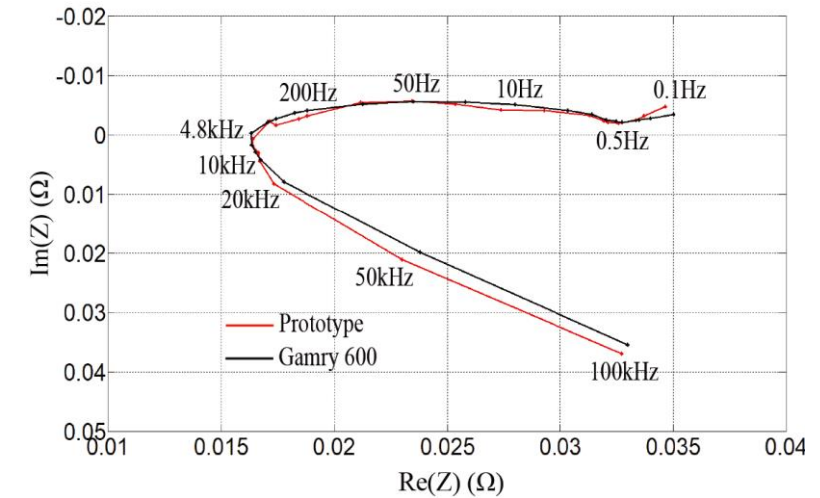
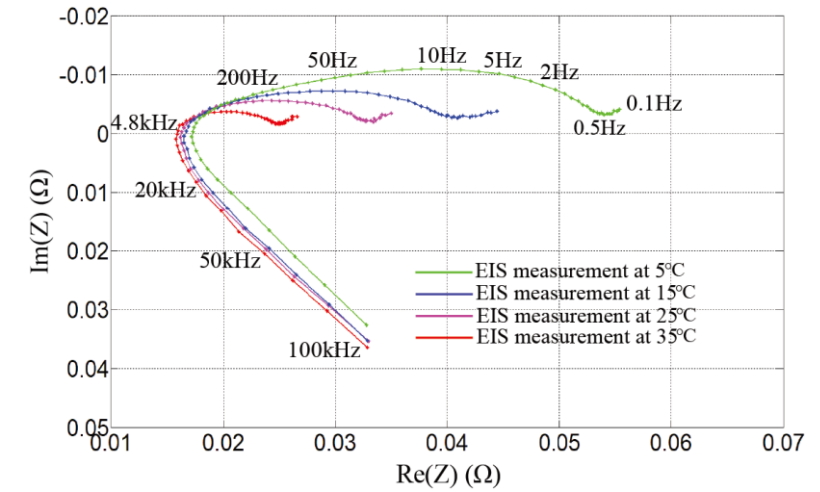
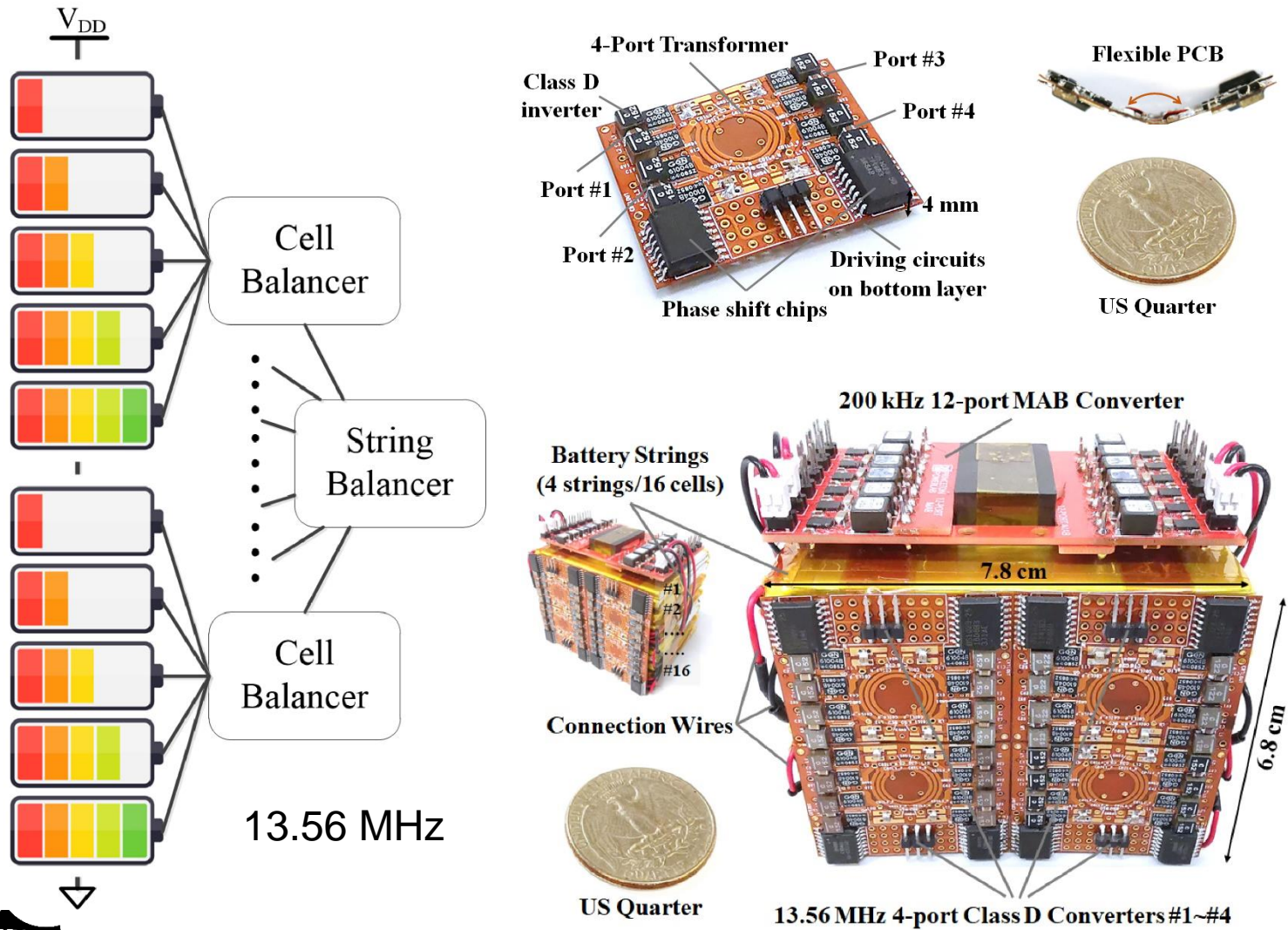
# Differential Power Processing for Data Storage



- P. Wang, Y. Chen, J. Yuan, R. C. N. Pilawa-Podgurski, M. Chen, "Differential Power Processing for Ultra-Efficient Data Storage," IEEE Transactions on Power Electronics, April 2021.



# Battery Balancer with On-line Impedance Spectroscopy



- M. Liu, Y. Chen, Y. Elasser, M. Chen, "Dual Frequency Hierarchical Modular Multilayer Battery Balancer Architecture," IEEE Transactions on Power Electronics, March 2021.





Grid Scale Energy Storage



Solar Photovoltaic

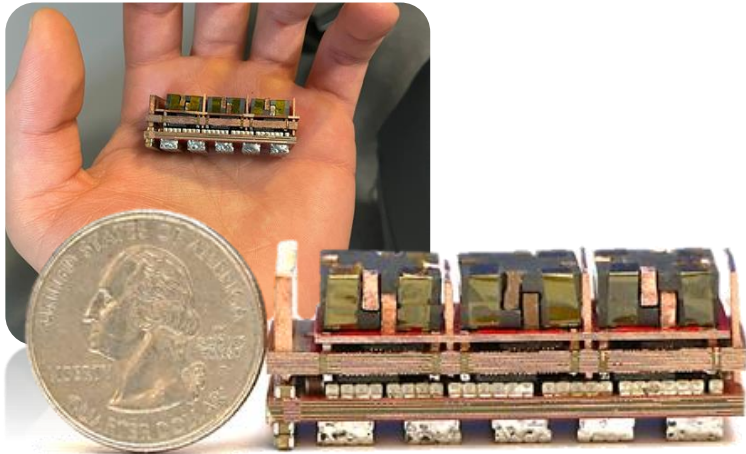


High Power LED Lighting

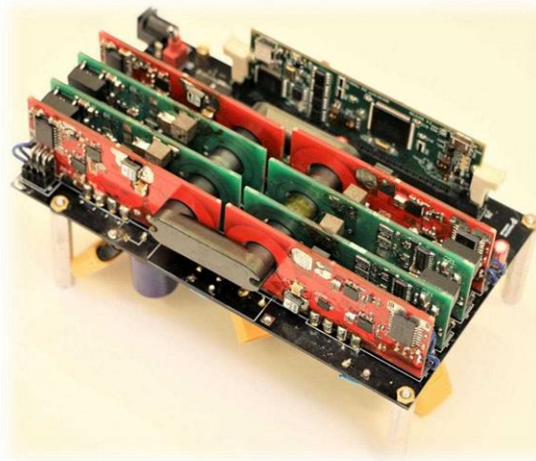
- Hardware, software, communication, thermal, algorithm and power co-design.
- Multi-input multi-output power management and grid interface.
- Efficiency, power density, reliability, cost, thermal.



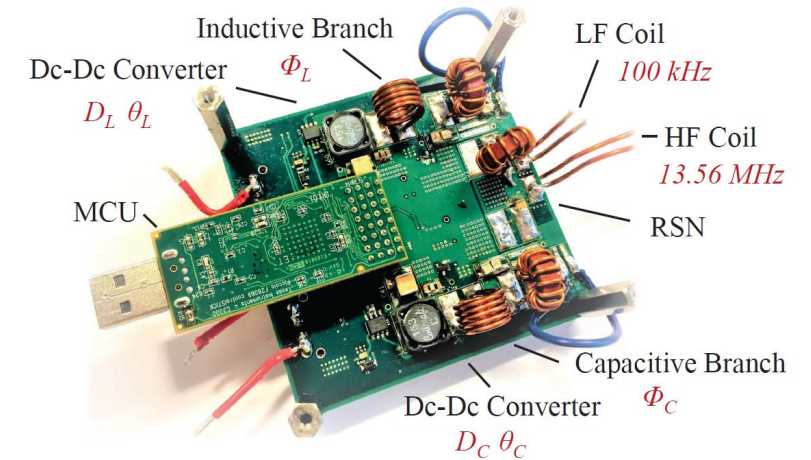
- **Extreme Performance:** Hybrid-Switched-Capacitor Architecture  
*Extreme Performance CPU Voltage Regulators*
- **Sophisticated Functions:** Control of MIMO Power Flow  
*Modeling and Control of Multiport Energy Routers*
- **Enabling New Applications:** Dual Frequency Wireless Power Transfer  
*Compensate for Impedance Variation with Reactance Steering Network*



CPU Voltage Regulator

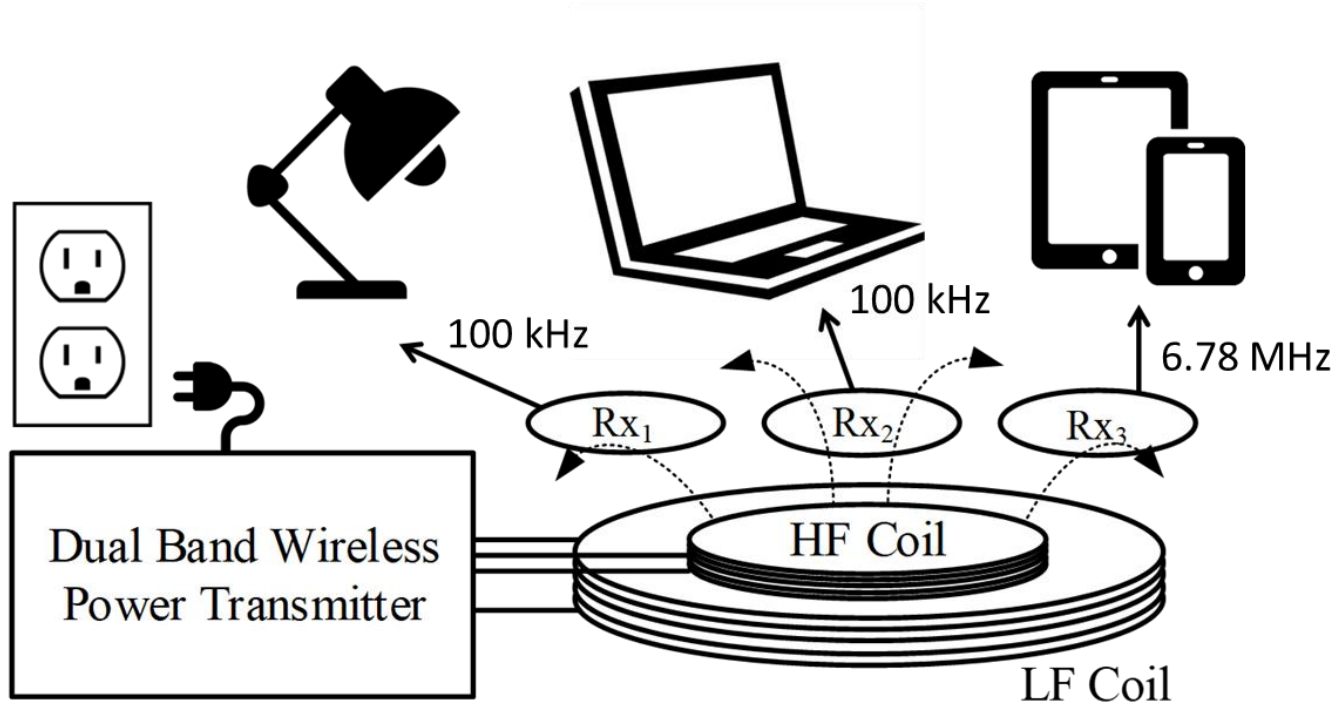


MIMO Energy Router



Dual-Band Wireless Power Transfer

## Dual-Band Multi-Receiver Wireless Power Transfer



## kHz wireless power transfer

- Higher efficiency
- Higher power transfer capability
- Large coil size
- Low tolerant to misalignment

## MHz wireless power transfer

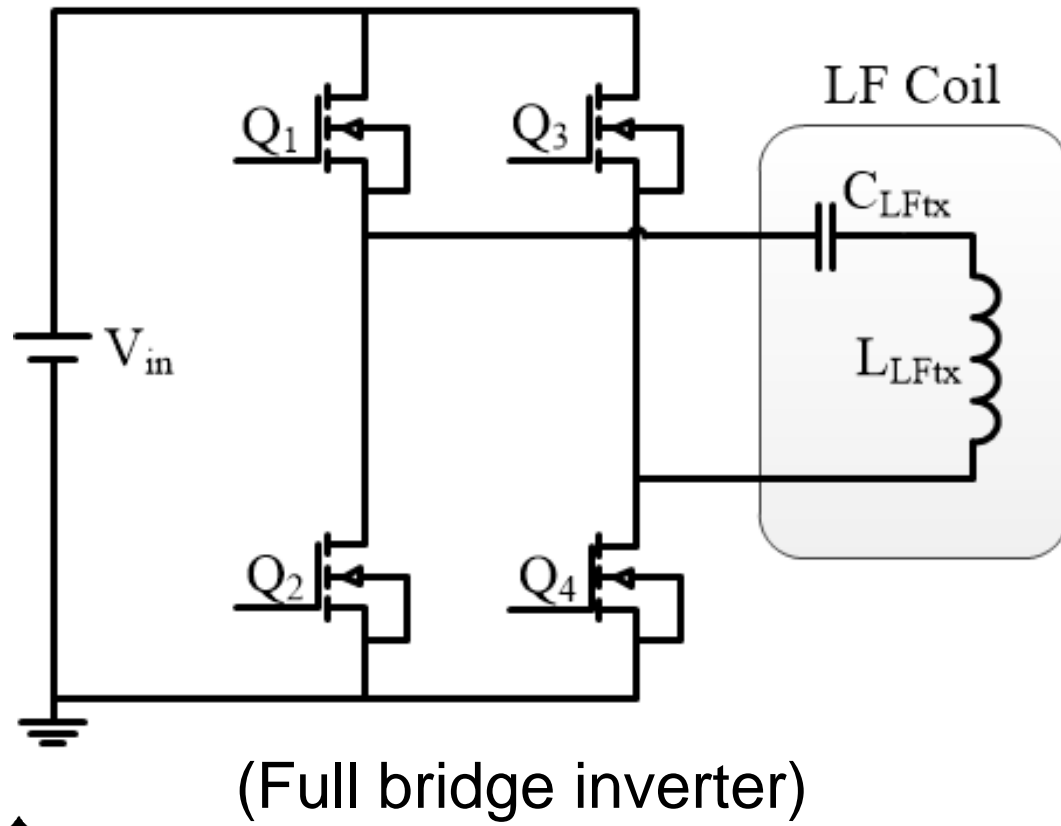
- Lower efficiency
- Lower power transfer capability
- Small coil size
- High tolerance to misalignment

Support multiple frequency bands with wide impedance variation

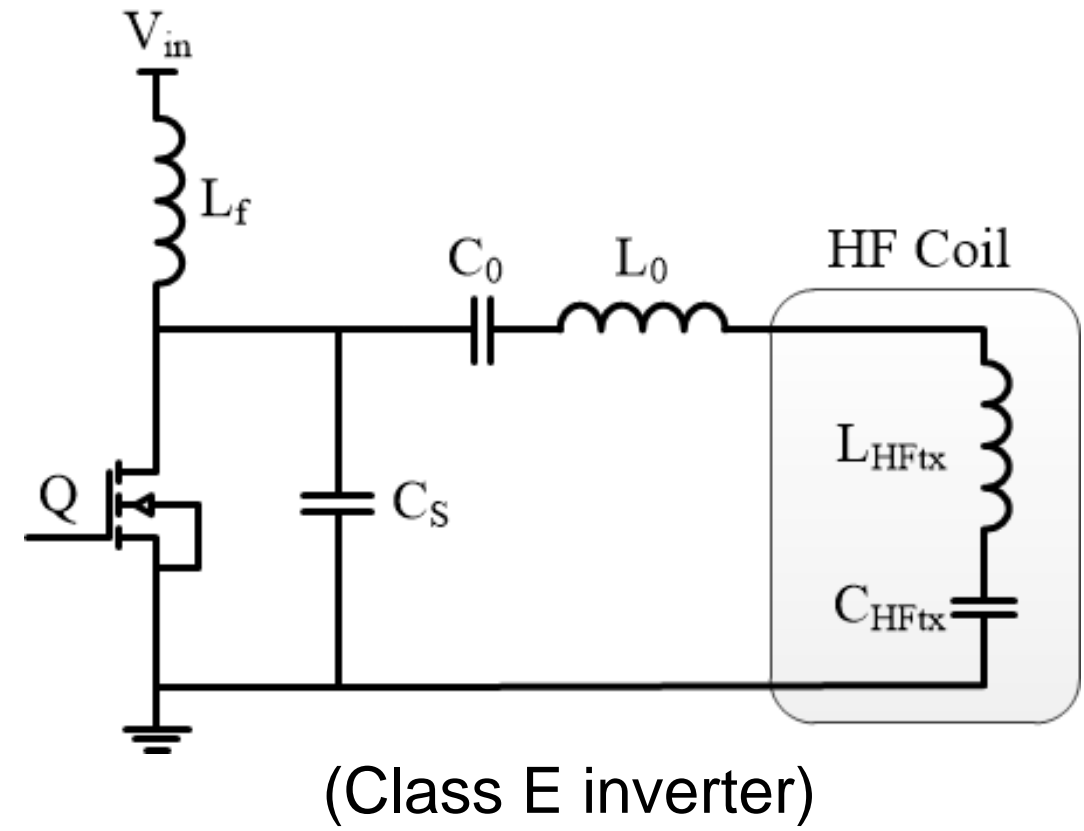




## Typical kHz WPT Transmitter

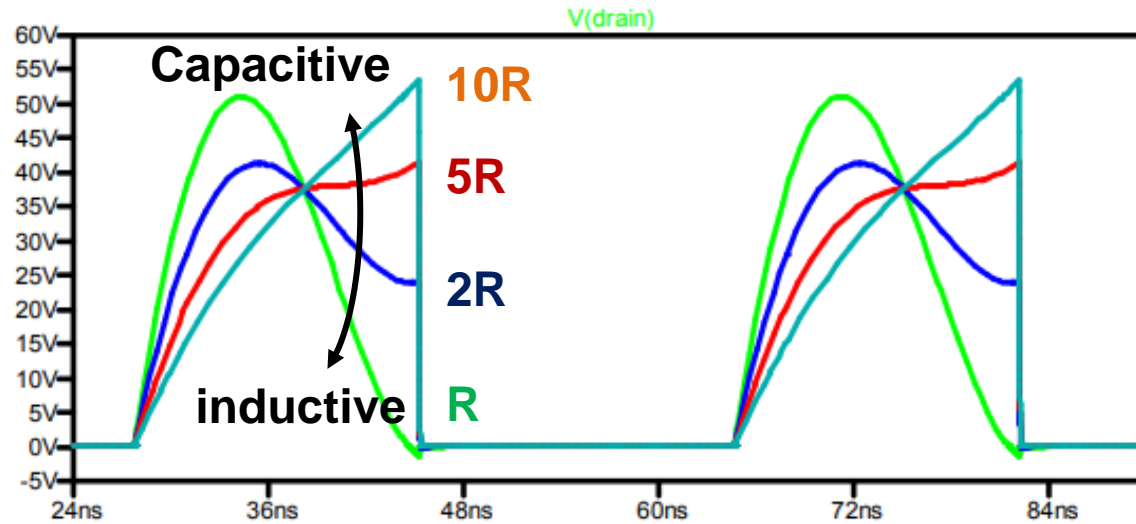


## Typical MHz WPT Transmitter

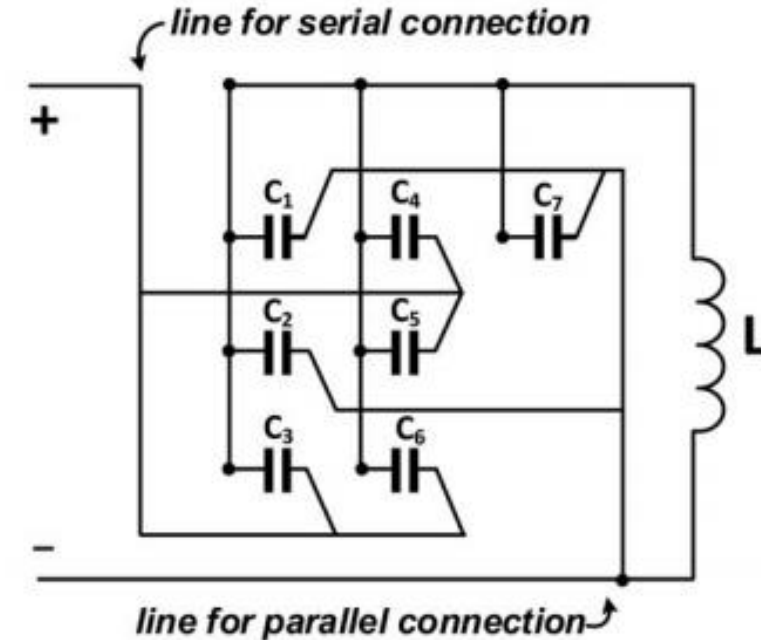


# Challenges of HF WPT with Single Switch PAs

- Co-location of multiple receivers induces large impedance variation
- Class-E PAs are sensitive to load impedance variation (resistive and reactive)

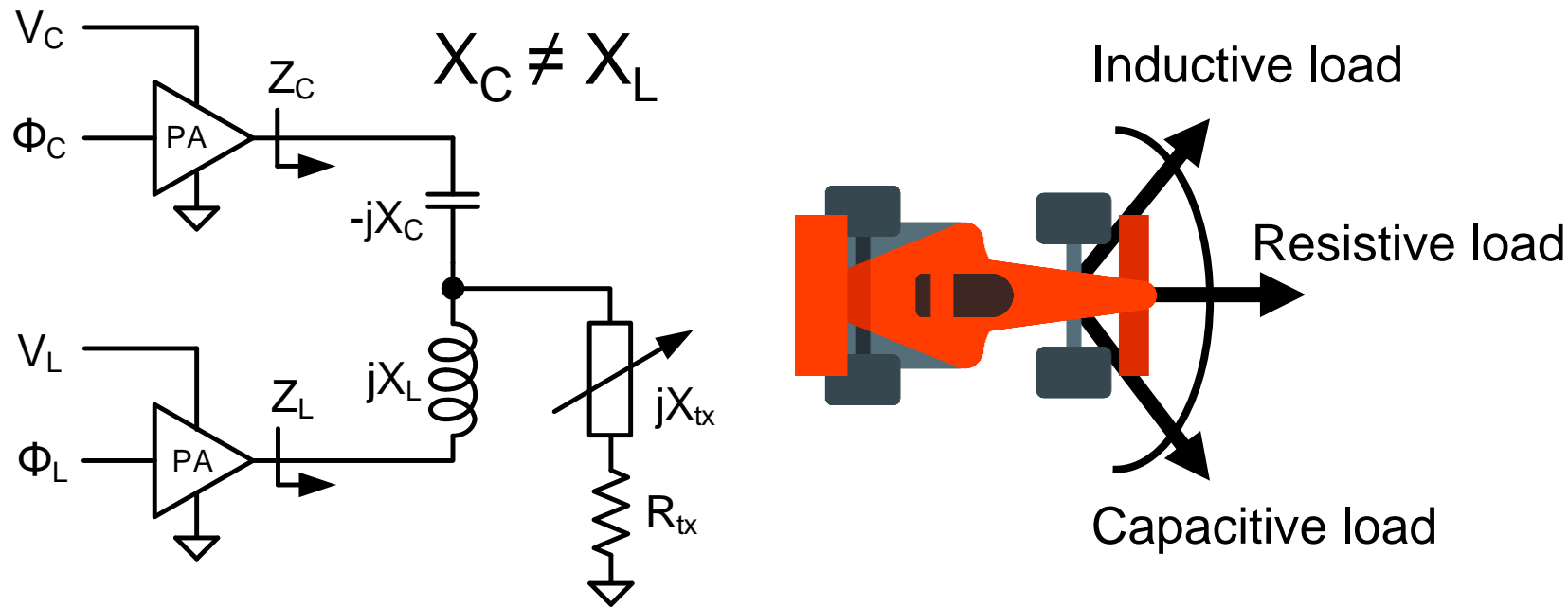


Drain voltage of Class-E PAs with impedance/resistance variation

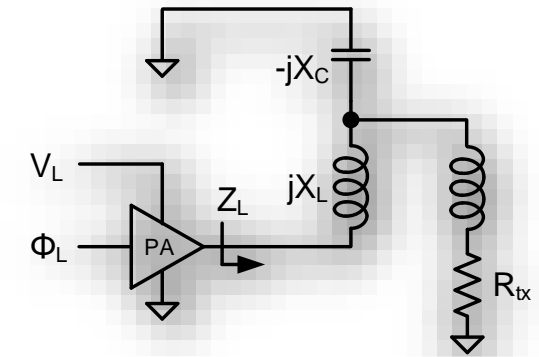


A tunable switched-capacitor matching network

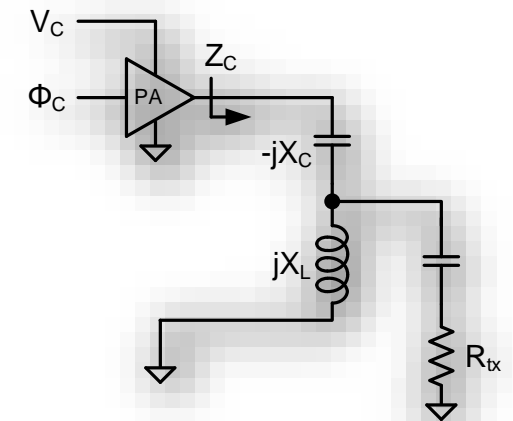
*Maintain pure resistive load for both PAs*



## Inductive load



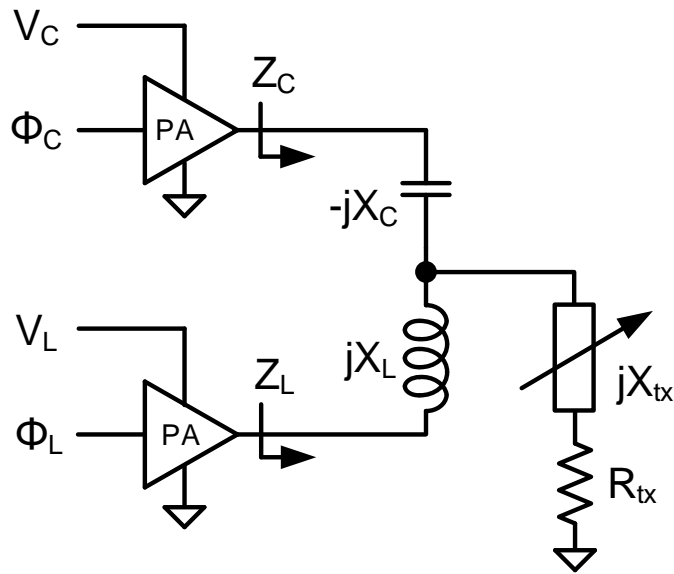
## Capacitive load



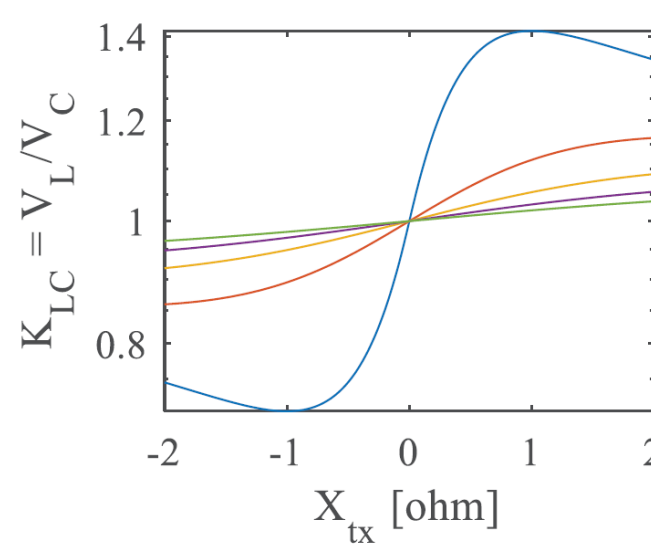
- Steering towards **capacitive** branch with **inductive** load
- Steering towards **inductive** branch with **capacitive** load
- Compensate for large reactance with small  $X_L$  and  $X_C$



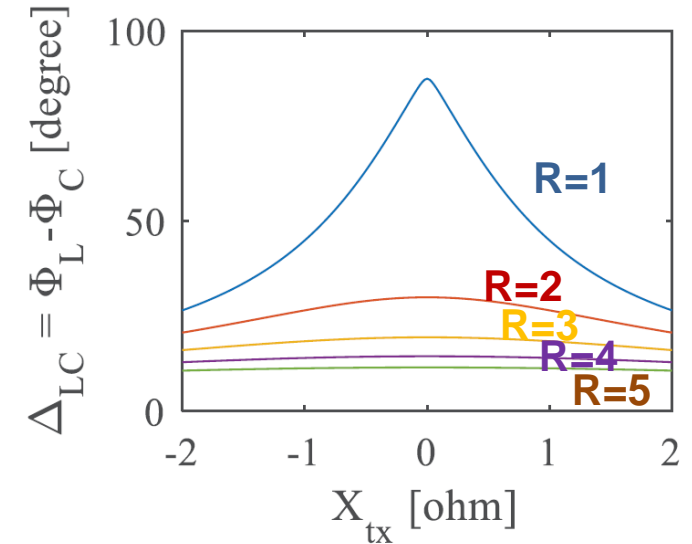




## Amplitude Ratio



## Phase Difference



## Amplitude Ratio

$$K_{LC} = \left| \frac{V_L}{V_C} \right| = \frac{X_O + X_{tx}}{X_{tx} \cos(\Delta_{LC}) + R_{tx} \sin(\Delta_{LC})}$$

## Phase Difference

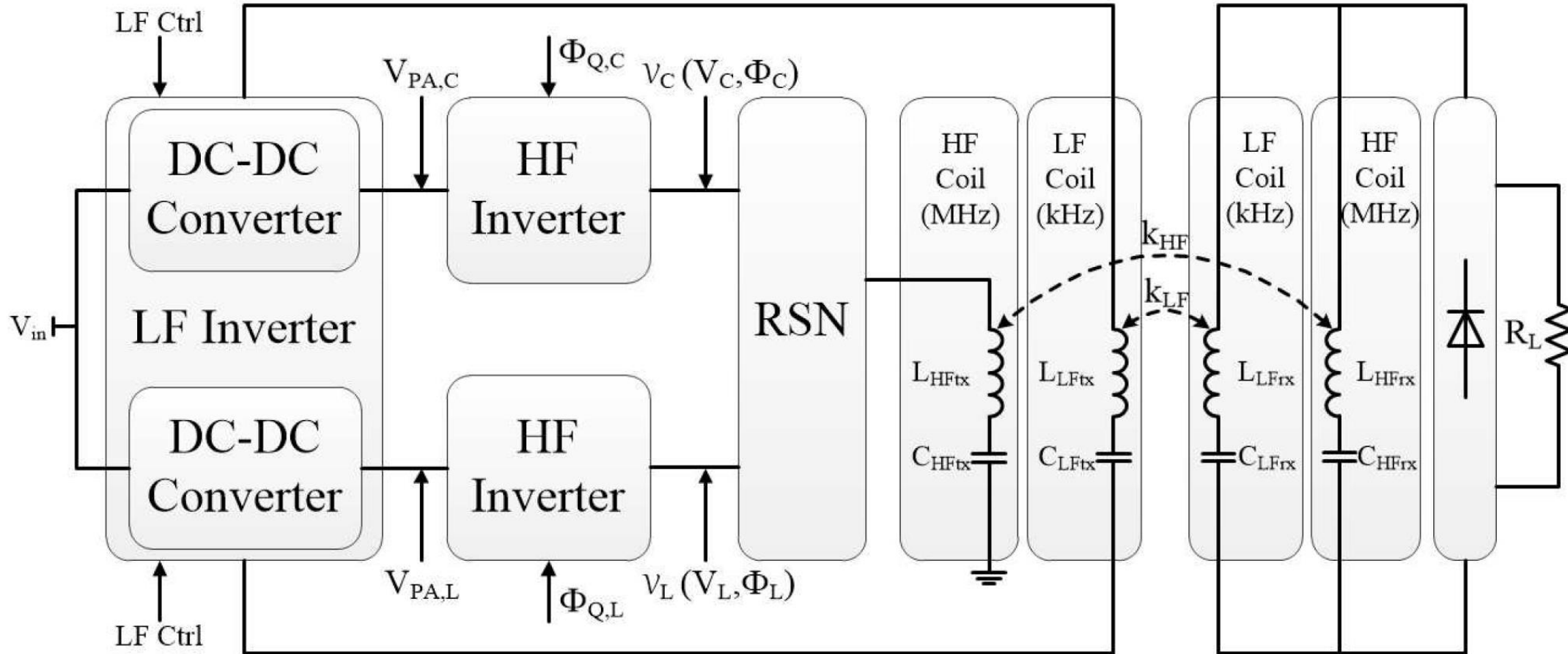
$$\Delta_{LC} = \Phi_L - \Phi_C = \arcsin \sqrt{\frac{X_O^2}{X_{tx}^2 + R_{tx}^2}}$$

$$\frac{1}{\sqrt{2}} < K_{LC} < \sqrt{2}$$

$$0^\circ < \Delta_{LC} < 90^\circ$$



- M. Liu, M. Chen, "Dual-Band Wireless Power Transfer with Reactance Steering Network and Reconfigurable Receivers," IEEE Transactions on Power Electronics, Jan. 2020.



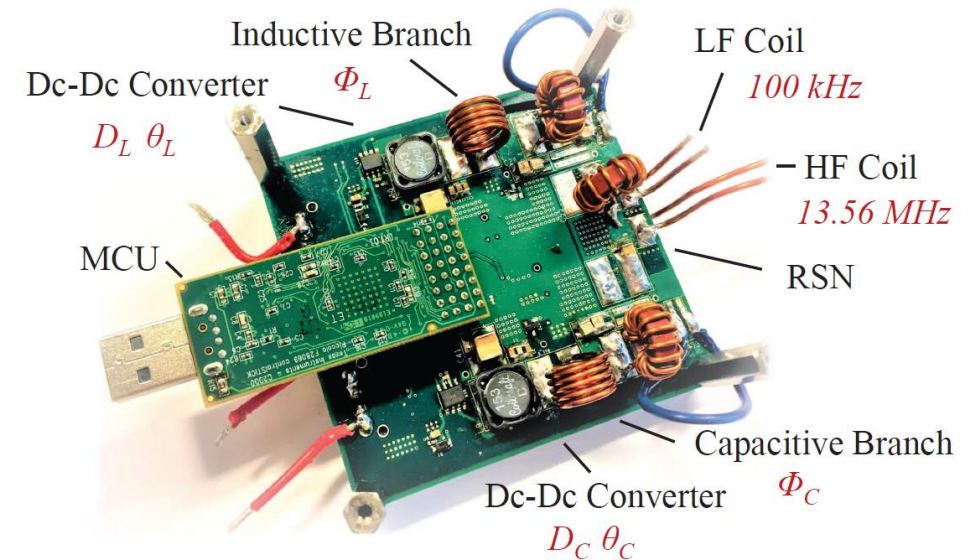
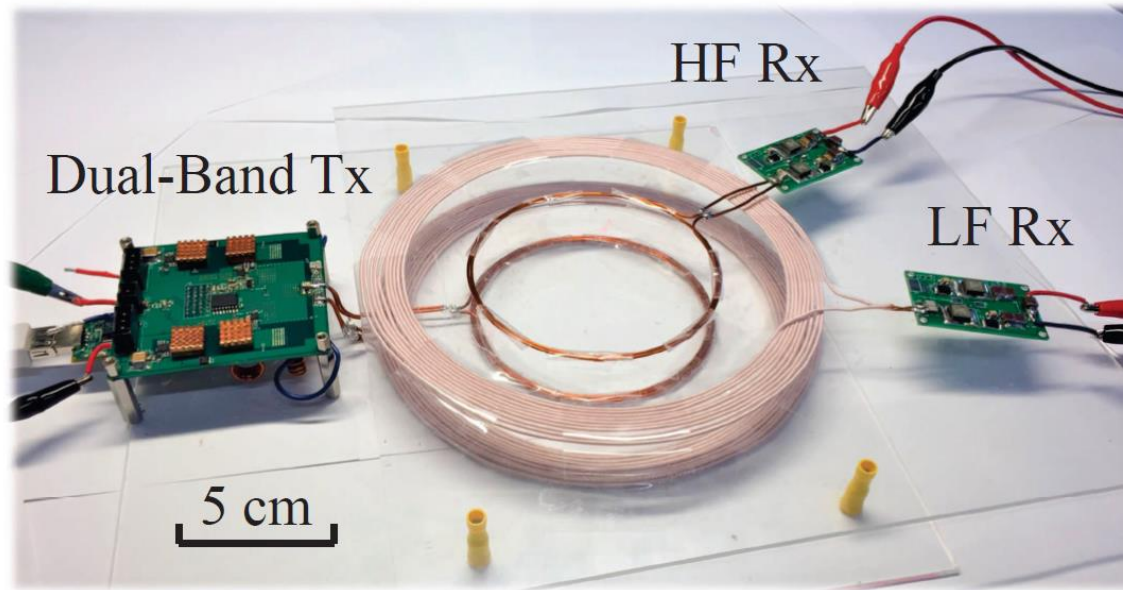
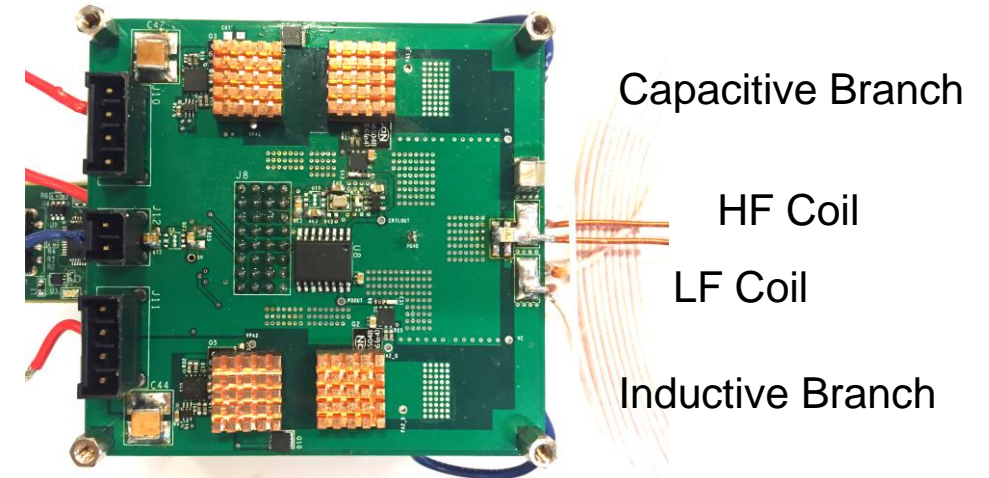
Merge LF and HF Transmitters, and create mutual advantages



- M. Liu, M. Chen, "Dual-Band Wireless Power Transfer with Reactance Steering Network and Reconfigurable Receivers," IEEE Transactions on Power Electronics, Jan. 2020.

# A Dual-Band Multi-Receiver WPT Prototype

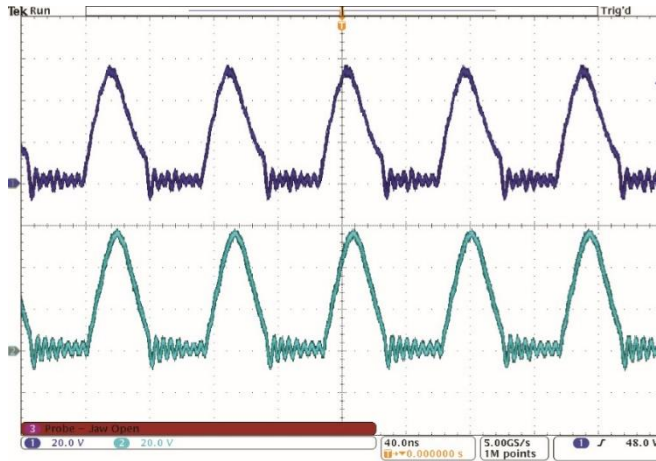
**Dual Band Operation:** 100 kHz and 13.56 MHz  
**Power Rating:** 65 W@100 kHz, 65 W@13.56 MHz  
**Input Voltage:** 50 V (up to 80 V)  
**Output Voltage:** 30 V@100 kHz, 30 V@13.56 MHz  
**Spacing:** 2.8 cm distance, up to 3 cm misalignments  
**Coil size:** Coil\_HF (D=10 cm), Coil\_LF (D=20 cm)



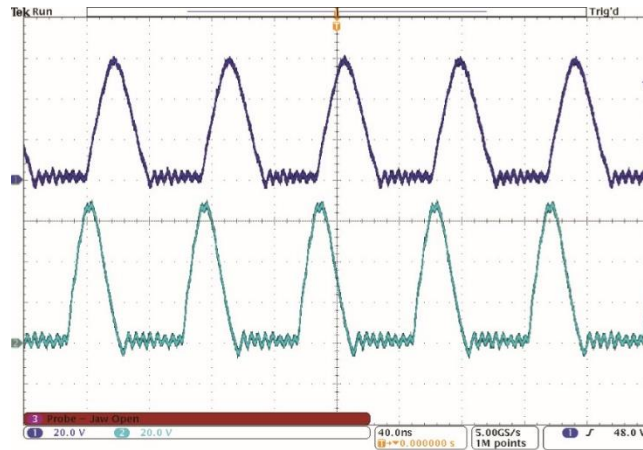
- M. Liu, M. Chen, "Dual-Band Wireless Power Transfer with Reactance Steering Network and Reconfigurable Receivers," IEEE Transactions on Power Electronics, Jan. 2020.



# ZVS of Both Class-E PAs across Very Wide Range

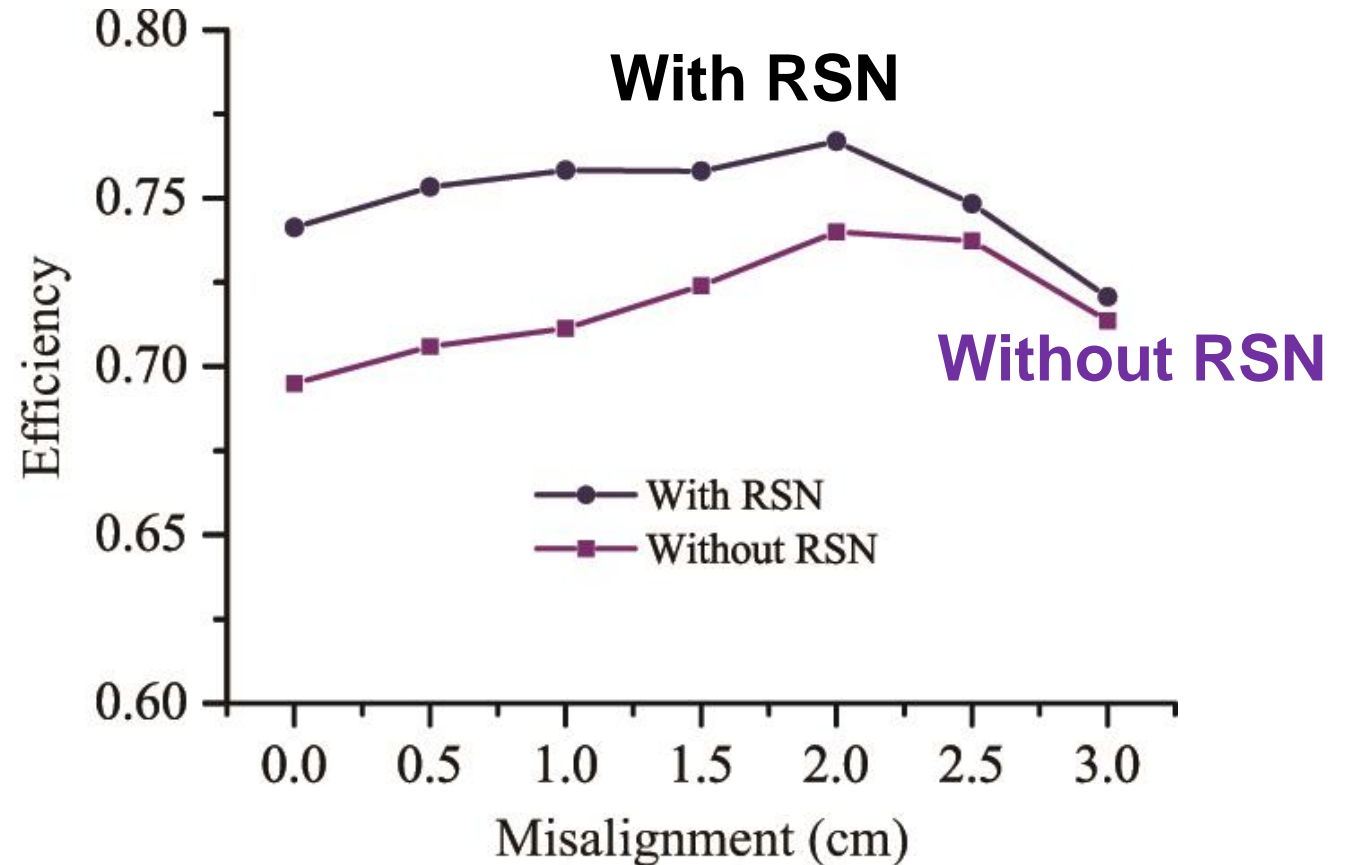


Example drain voltage without RSN



Example drain voltage with RSN

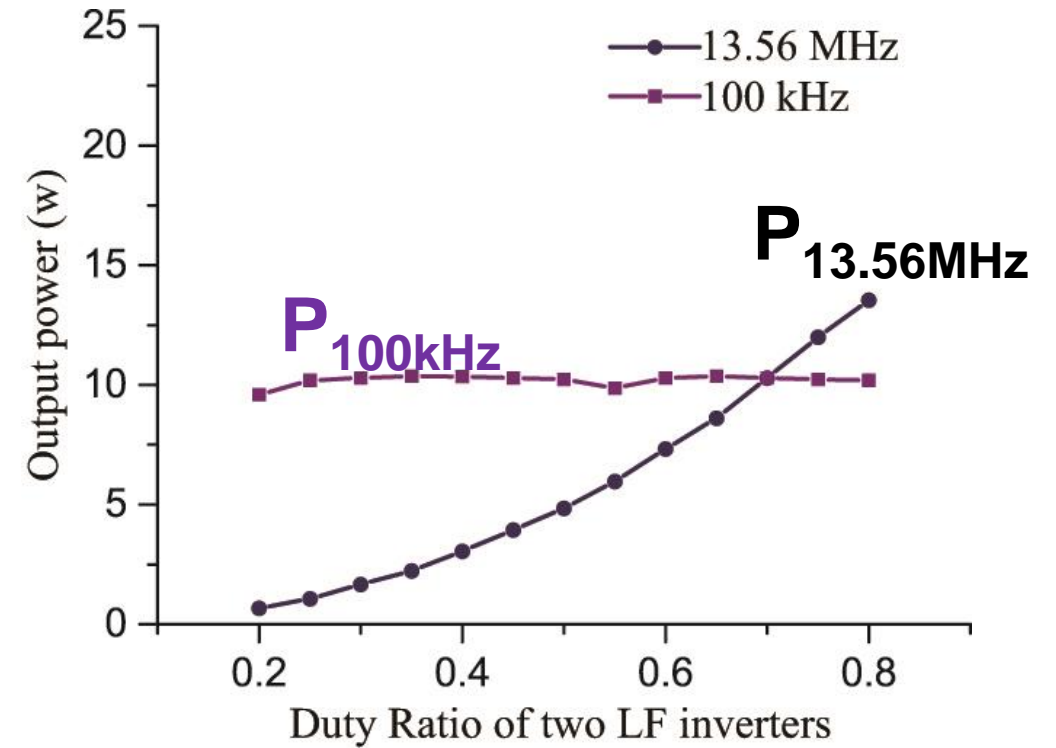
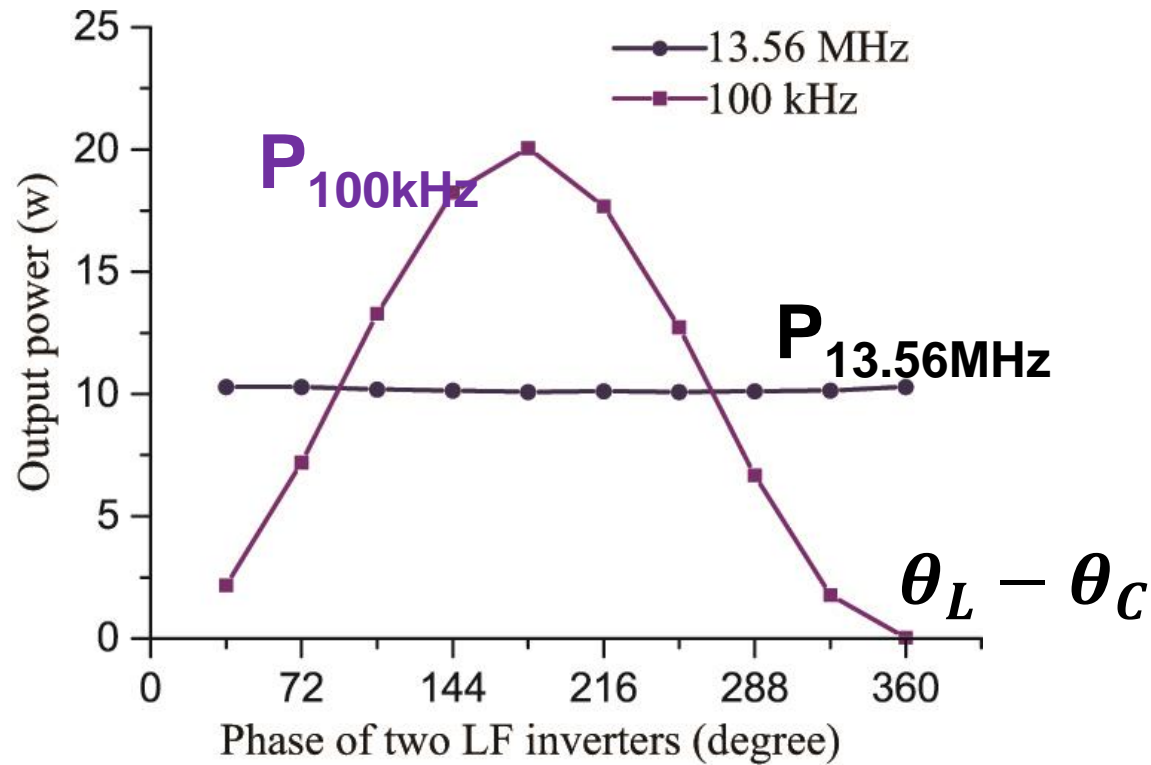
- Efficiency vs. misalignment (0 ~ 3 cm)
- Fixed output power 30W
- Reactance range from  $0j \Omega$  to  $80j \Omega$



# Decoupled Modulation of the Two Frequency Bands

- Modulating power at 100 kHz
- Maintaining 10 W at 13.56 MHz

- Modulating power at 13.56 MHz
- Maintaining 10 W at 100 kHz



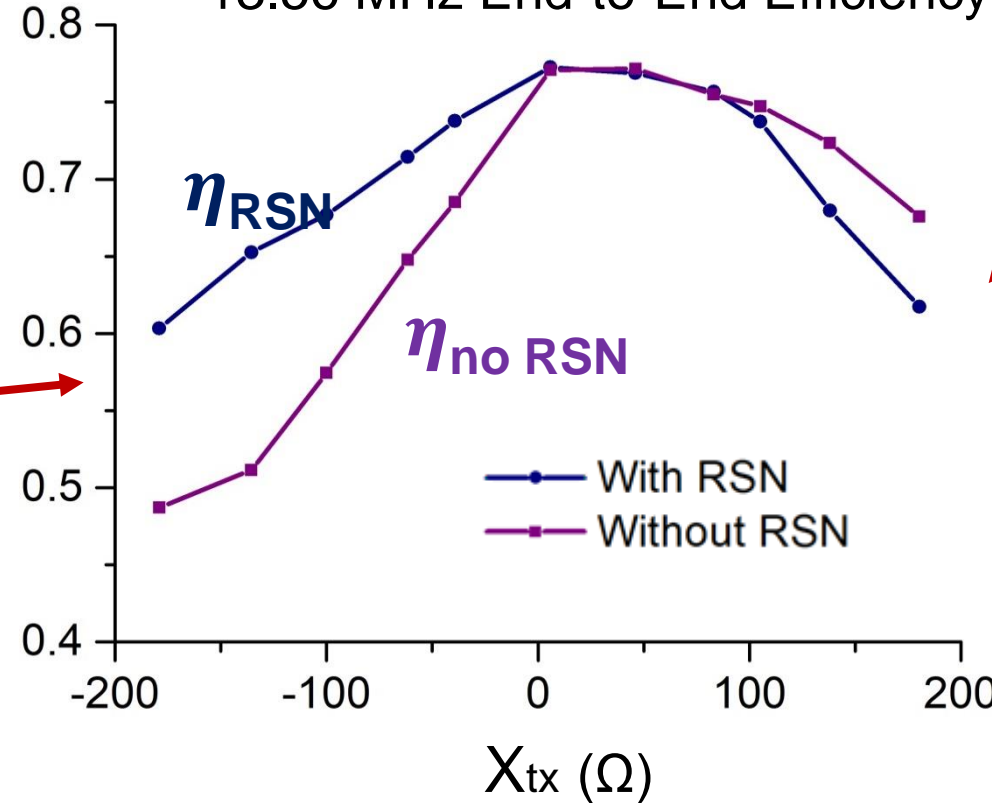
- M. Liu, M. Chen, "Dual-Band Wireless Power Transfer with Reactance Steering Network and Reconfigurable Receivers," IEEE Transactions on Power Electronics, Jan. 2020.

# HF WPT Efficiency with “Very” Reactive Load

- RSN significantly improves the HF WPT efficiency with capacitive  $X_{tx}$ .
- RSN sacrifices more loss with very inductive load (due to circulating current).

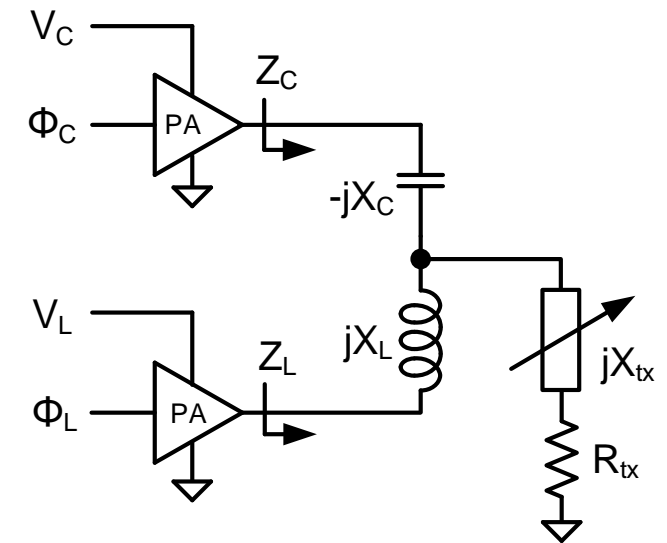
R: 50  $\Omega$   
X: -200  $\Omega$  to +200  $\Omega$

13.56 MHz End-to-End Efficiency



12% higher efficiency with “very” capacitive load

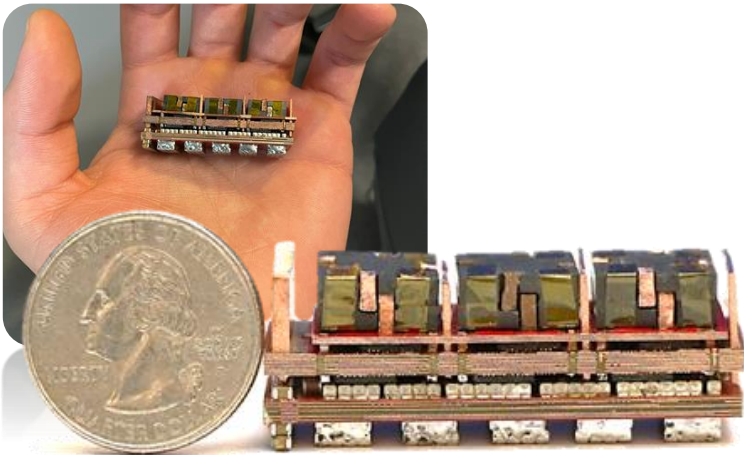
4% lower efficiency with “very” inductive load



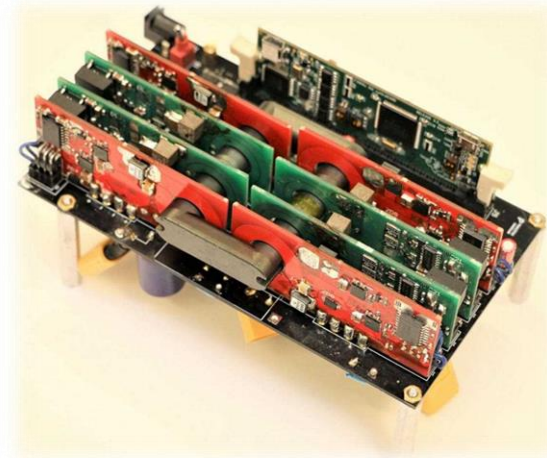


# Unlock the Potential of WBG Semiconductor Devices

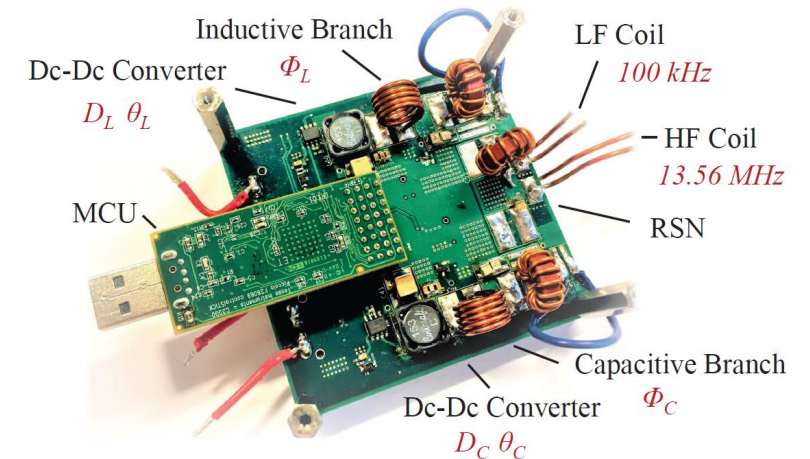
- “Drop and replace” designs only leverage the “efficiency” benefits
- WBG devices enables architectural level innovations, including:
  - Very-small-footprint: more compact packaging and better thermal
  - Ultra-fast-switching: more precise control and timing, smaller passives
  - Extended-design-space: reusing devices for multiple purposes at HF



CPU Voltage Regulator



MIMO Energy Router



Dual-Band Wireless Power Transfer

# Related Publications

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## 48V-1V CPU Voltage Regulator

- J. Beak et al., “Vertical Stacked 48V-1V CPU Voltage Regulator with 91.1% Efficiency, 1 A/mm<sup>2</sup> Current Density and 1,000 W/in<sup>3</sup> Power Density”, IEEE Transactions on Power Electronics, in preparation.
- J. Baek, Y. Elasser, and M. Chen, “3D LEGO-PoL: A 93.3% Efficient 48V-1.5V 450A Merged-Two-Stage Hybrid Switched-Capacitor Converter with 3D Vertical Coupled Inductors,” APEC 2021.
- M. Chen and C. R. Sullivan, “Unified Models for Coupled Inductors Applied to Multiphase PWM Converters,” IEEE Transactions on Power Electronics, accepted.
- Y. Chen, H. Cheng, D. Giuliano, M. Chen, “A 93.7% Efficient 400A 48V-1V Merged-Two-Stage Hybrid Switched-Capacitor Converter with 24V Virtual Intermediate Bus and Coupled Inductors,” APEC 2021.

## MIMO Energy Router

- P. Wang and M. Chen, “Towards Power FPGA: Architecture, Modeling and Control of Multiport Power Converters,” IEEE COMPEL, Padua, Italy, June 2018.
- Y. Chen, P. Wang, Y. Elasser, M. Chen, “Multicell Reconfigurable Multi-Input Multi-Output Energy Router Architecture,” IEEE Transactions on Power Electronics, Dec. 2020.
- P. Wang, Y. Chen, J. Yuan, R. C. N. Pilawa-Podgurski, M. Chen, “Differential Power Processing for Ultra-Efficient Data Storage,” IEEE Transactions on Power Electronics, April 2021.

## Wireless Power Transfer

- M. Liu and M. Chen, “Dual-Band Wireless Power Transfer with Reactance Steering Network and Reconfigurable Receivers,” IEEE Transactions on Power Electronics, Jan. 2020.

